

# Dark Energy and the Homogeneous Universe

暗能量及宇宙整體之膨脹

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This is a series of 3 talks.

Today: Dark energy and the homogeneous  
universe

July 11: Dark matter and the large scale  
structure of the universe

July 18: Inflation and the early universe



## Outline

**Basic concepts:** a homogeneous, isotropic and expanding universe.

**Measurements:** how do we measure the universe's expansion history?

**Dynamics:** what determines the expansion rate?

**Dark energy:** a surprising recent finding.



There is by now much evidence for  
homogeneity and isotropy.

There is also firm evidence for an  
expanding universe.



scale  $\sim 10^{23}$  cm

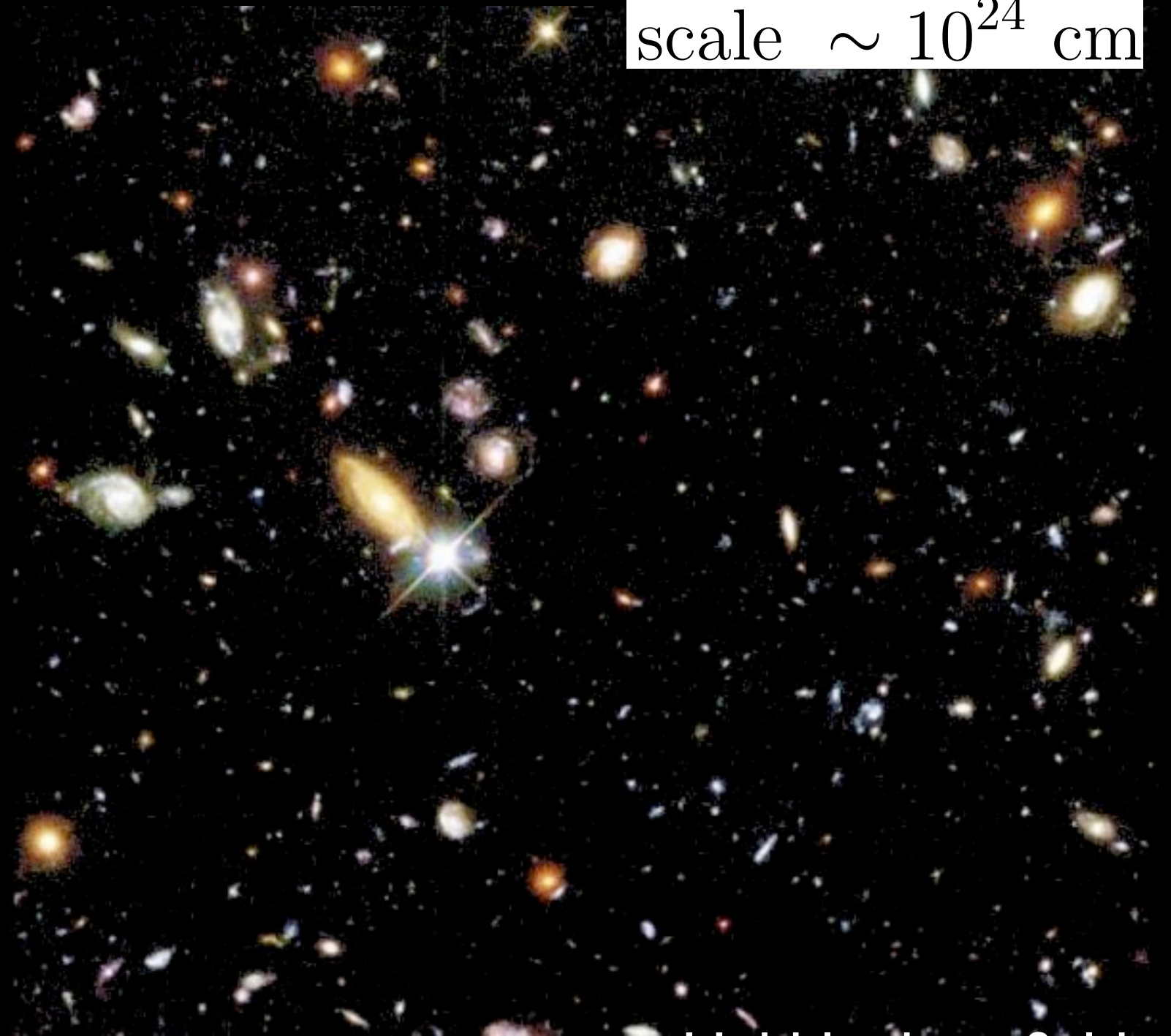
NGC 1042 / MCG -2 7 54 / IRAS 02379-0838

SDSS *gr<sub>i</sub>* image

2.0 arcmin

Blandton & Hogg

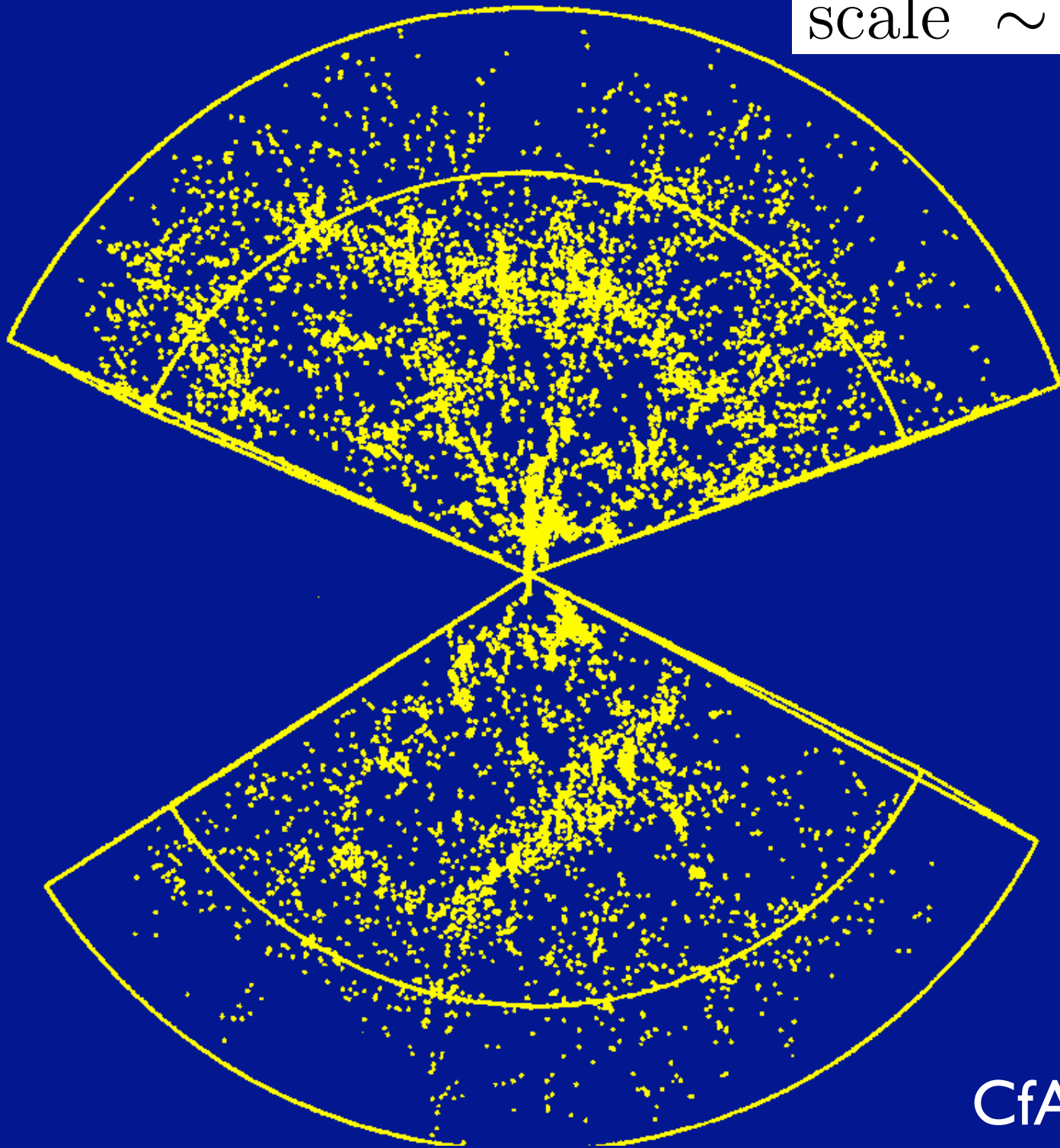
scale  $\sim 10^{24}$  cm



Hubble deep field



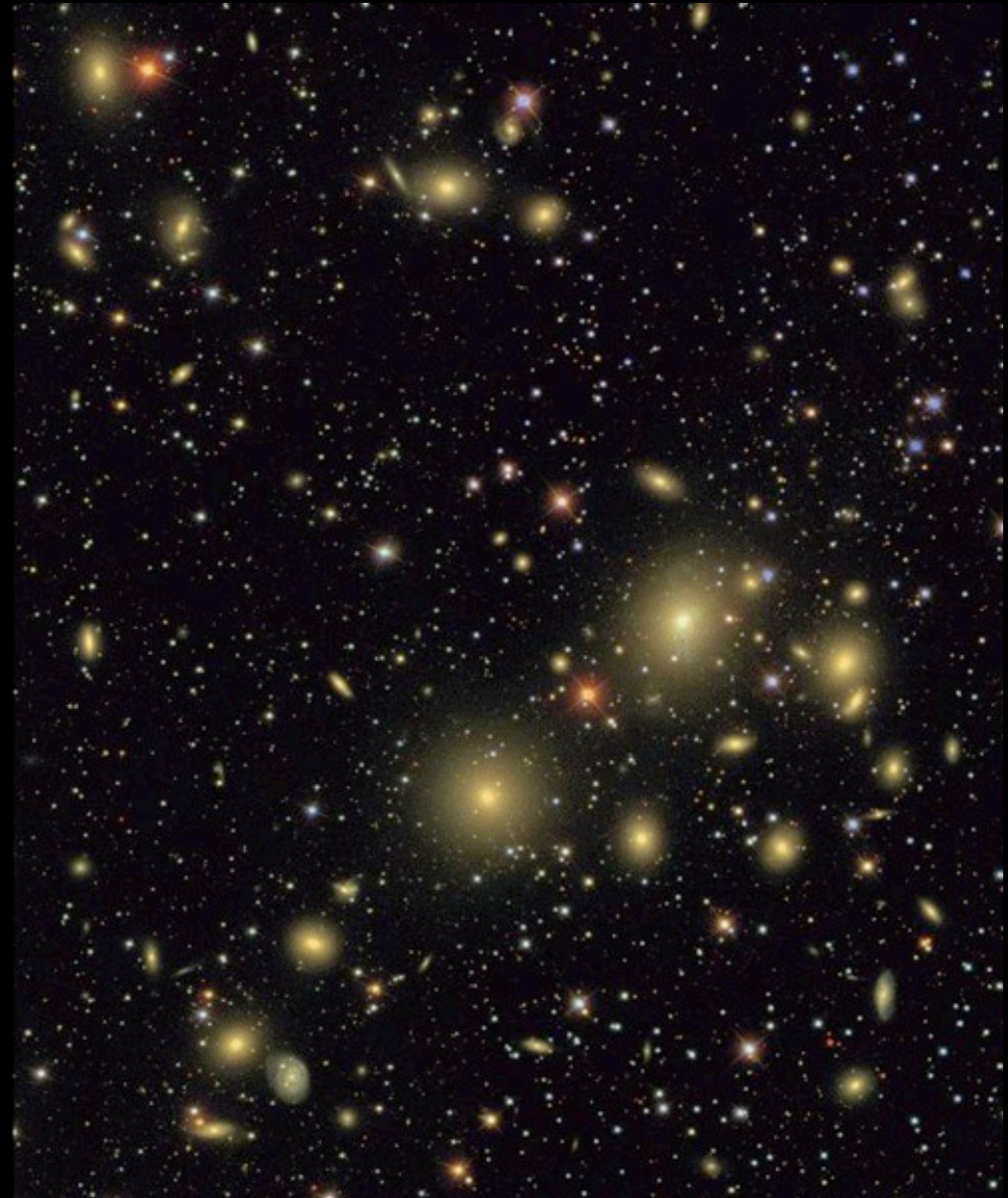
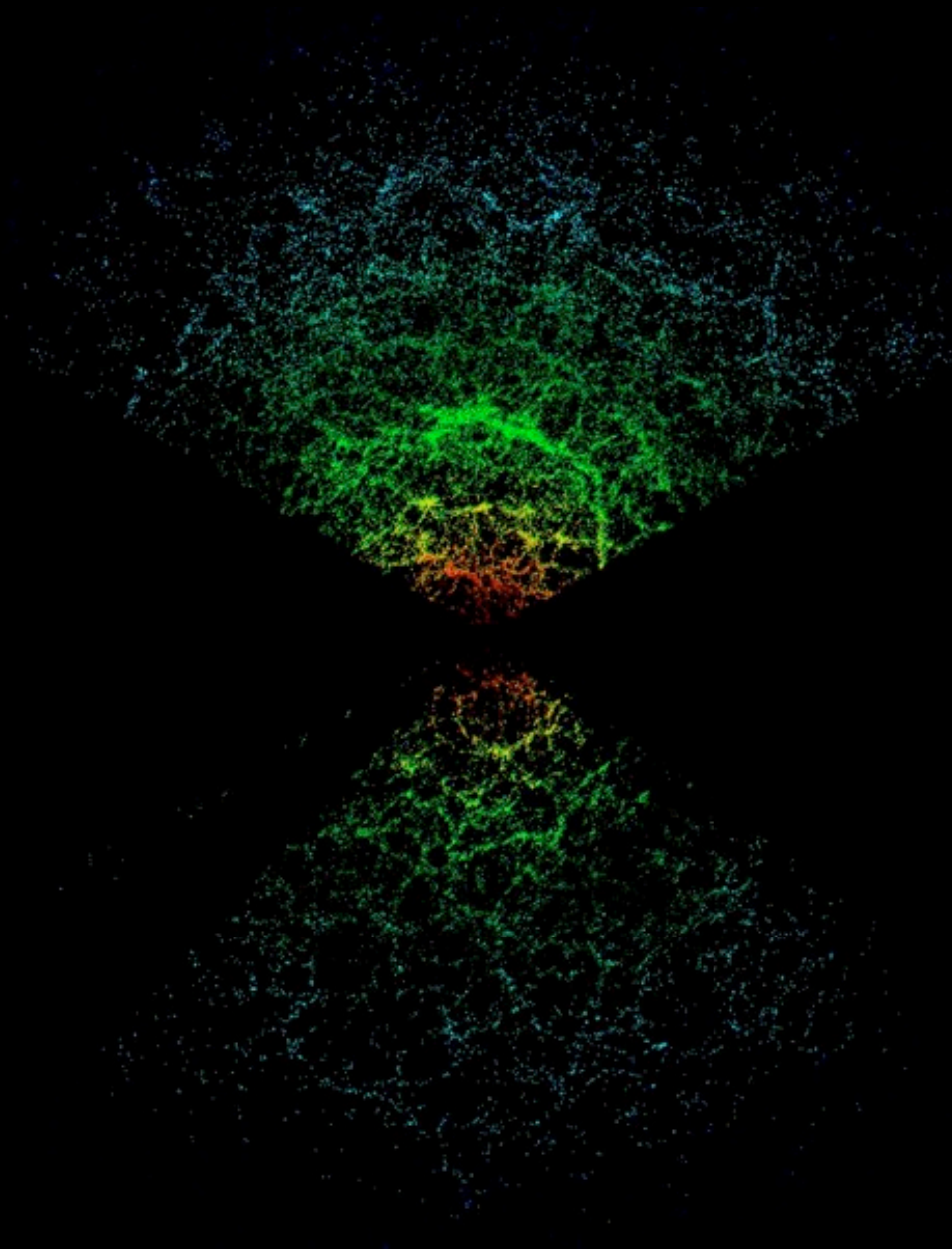
scale  $\sim 10^{25}$  cm



CfA survey

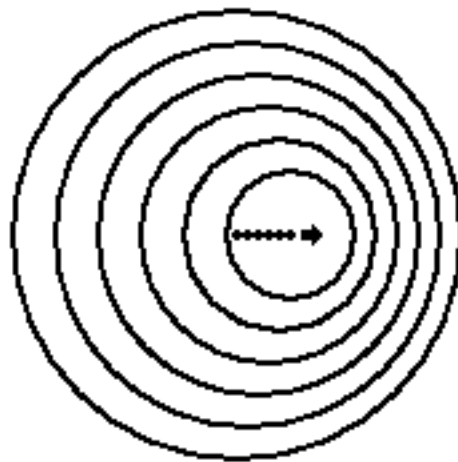
# Sloan Digital Sky Survey

scale  $\sim 10^{26}$  cm





OBJECT RECEDING:  
LONG RED WAVES



OBJECT APPROACHING:  
SHORT BLUE WAVES



Ned Wright



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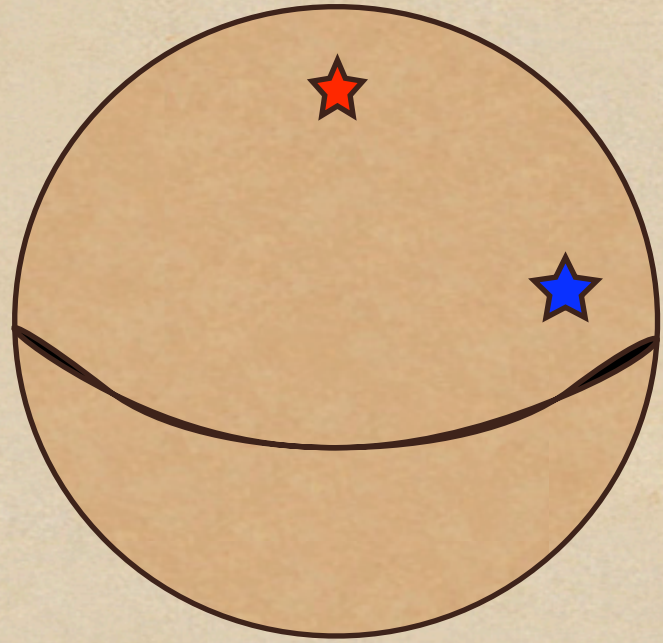
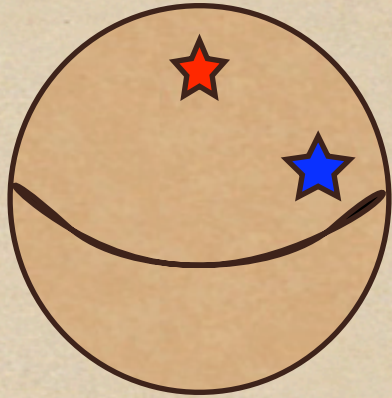


There is by now much evidence for  
homogeneity and isotropy.

There is also firm evidence for an  
expanding universe.

But how should we think about it?







## Frequently Asked Questions:

1. What is the universe expanding into?
2. Where is the center of expansion?
3. Is our galaxy itself expanding?



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1. What is the universe expanding into?

Nothing.

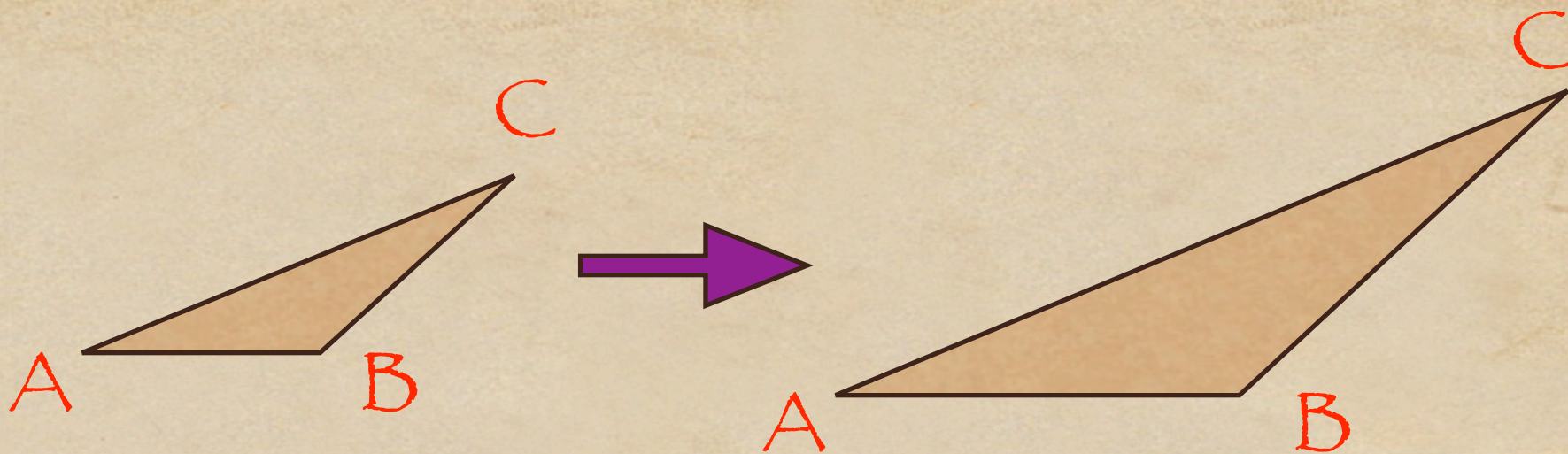
2. Where is the center of expansion?

Everywhere and nowhere.

3. Is our galaxy itself expanding?

No.





$$d_{AC} = 2 d_{AB}$$

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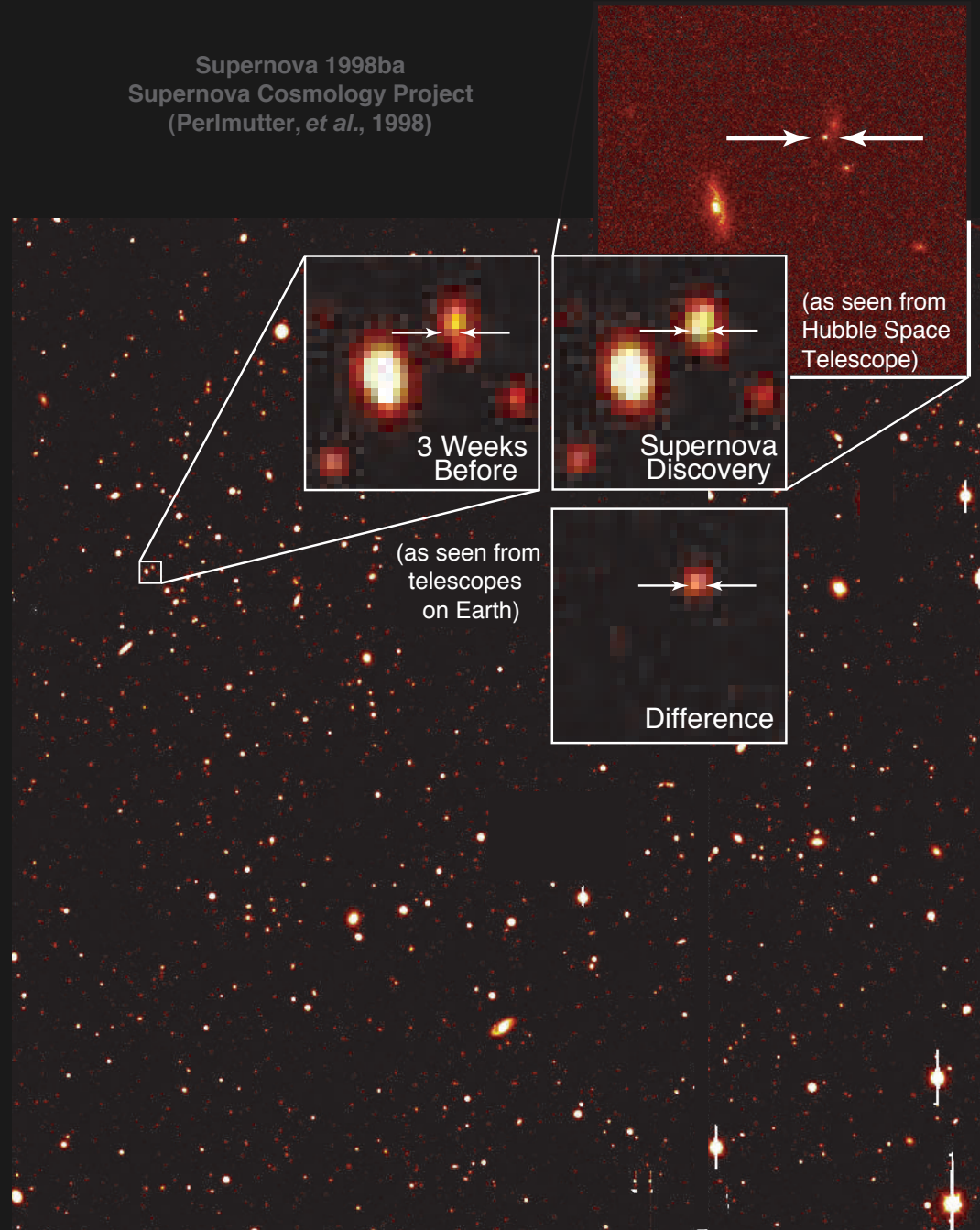
Therefore:

$$\frac{\Delta d_{AC}}{\Delta t} = 2 \frac{\Delta d_{AB}}{\Delta t}$$

Hubble law: Velocity  $\propto$  Distance



Supernova 1998ba  
Supernova Cosmology Project  
(Perlmutter, *et al.*, 1998)

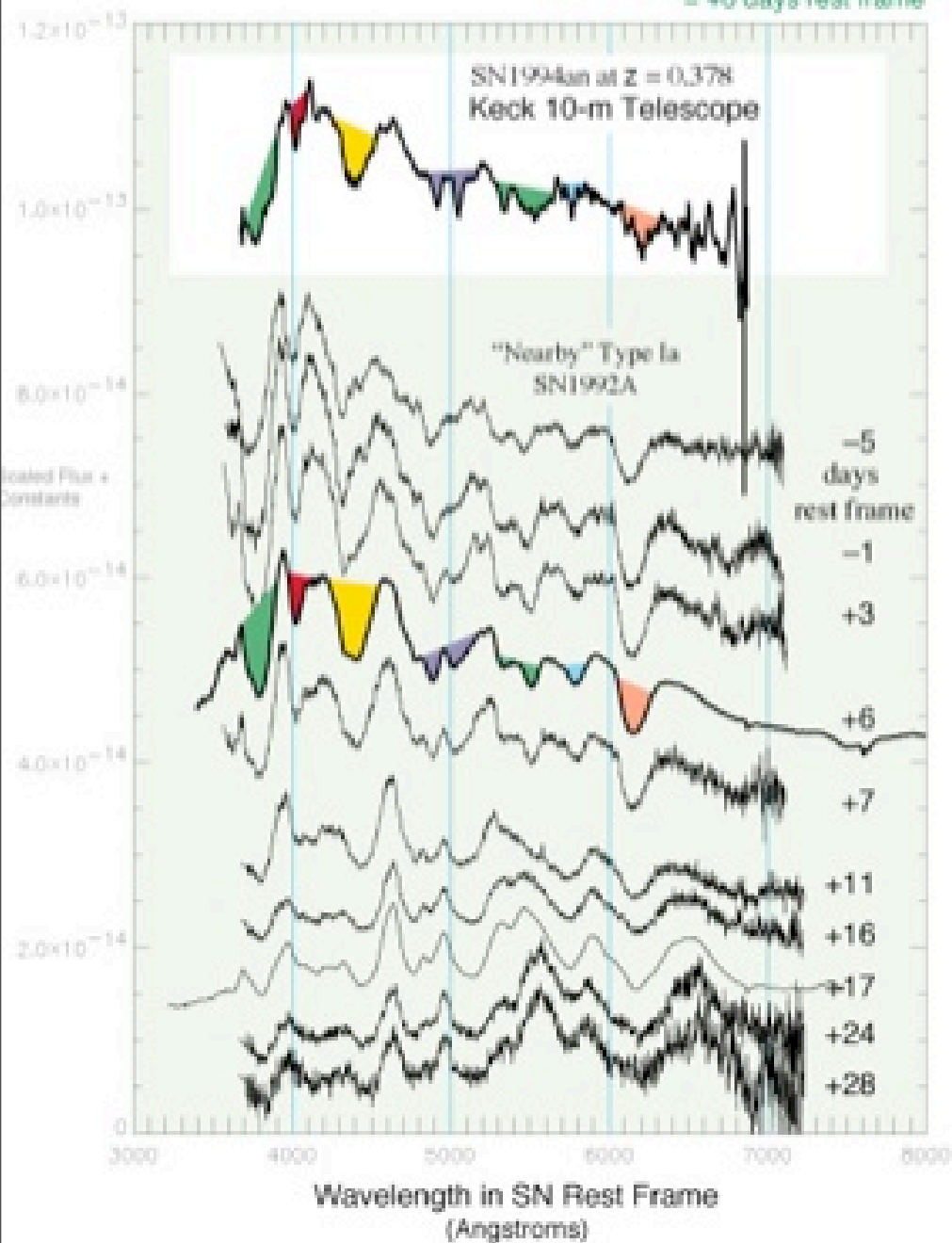


Supernova 超新星 as standard candle



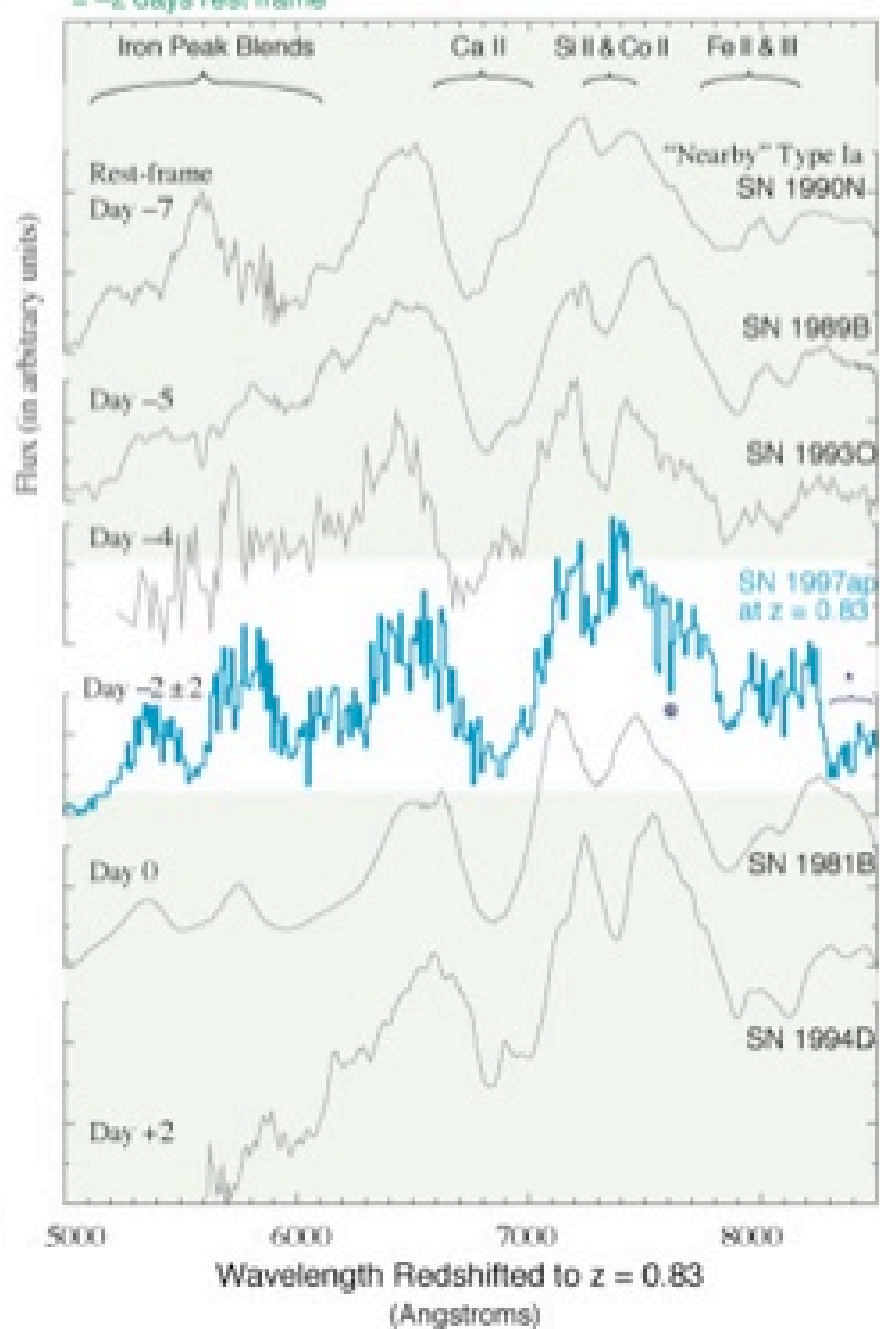
at  $z = 0.38 \dots$

+9 days past max observer frame  
= +6 days rest frame



$\dots$  at  $z = 0.83$

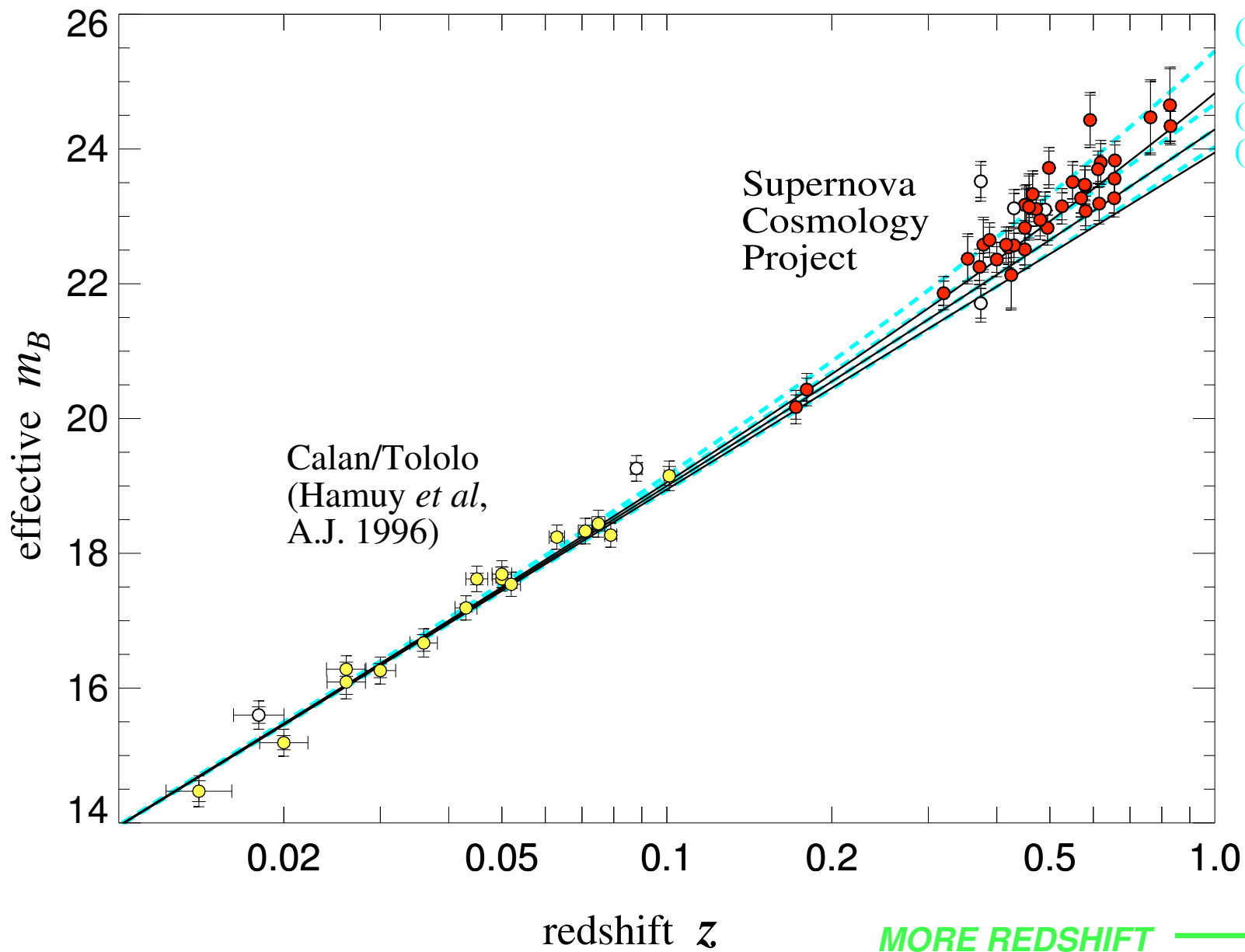
-4 days (before) max observer frame  
= -2 days rest frame





Perlmutter, *et al.* (1998)

$(\Omega_M, \Omega_\Lambda) =$   
(0, 1)  
(0.5, 0.5) (0, 0)  
(1, 0) (1, 0)  
(1.5, -0.5) (2, 0)  
Flat  $\Lambda = 0$



**MORE REDSHIFT**  $\longrightarrow$   
(More total expansion of universe  
since the supernova explosion)

See also Riess *et al.* 98

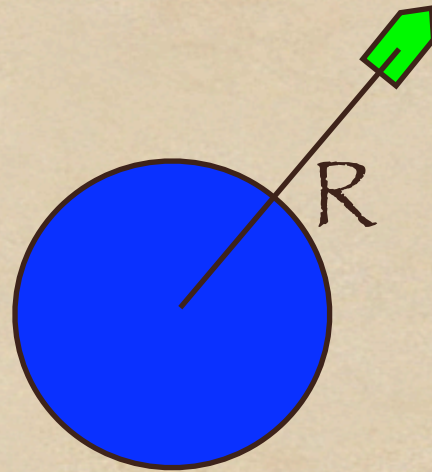


## Age of Universe

Slope = Distance/Velocity = 10 billion years



**Dynamics:** what determines the expansion rate and how it changes with time?



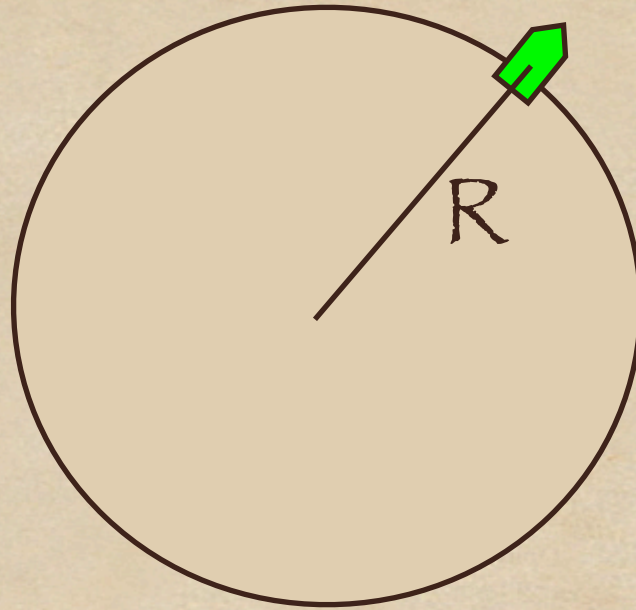
Secondary school physics:

$$\frac{1}{2}mv^2 - \frac{GMm}{R} = E$$

For simplicity set  $E = 0$  :  $\frac{1}{2}v^2 = \frac{GM}{R}$



Apply to the expanding universe:



$$\frac{1}{2}v^2 = \frac{GM}{R}, \quad \text{but remember : } M = \frac{4\pi}{3}R^3\rho$$



Important equation:  $\frac{1}{2}v^2 = \frac{GM}{R}$  where  $M = \frac{4\pi}{3}R^3\rho$

Example 1 - ordinary matter

$$\rho \propto \frac{3}{4\pi R^3} \quad (M = \text{constant}) \quad \implies v^2 \propto \frac{1}{R}$$

Therefore :  $v \downarrow \iff R \uparrow$

Example 2 - cosmological constant

$$\rho = \text{constant} \implies v^2 \propto R^2$$

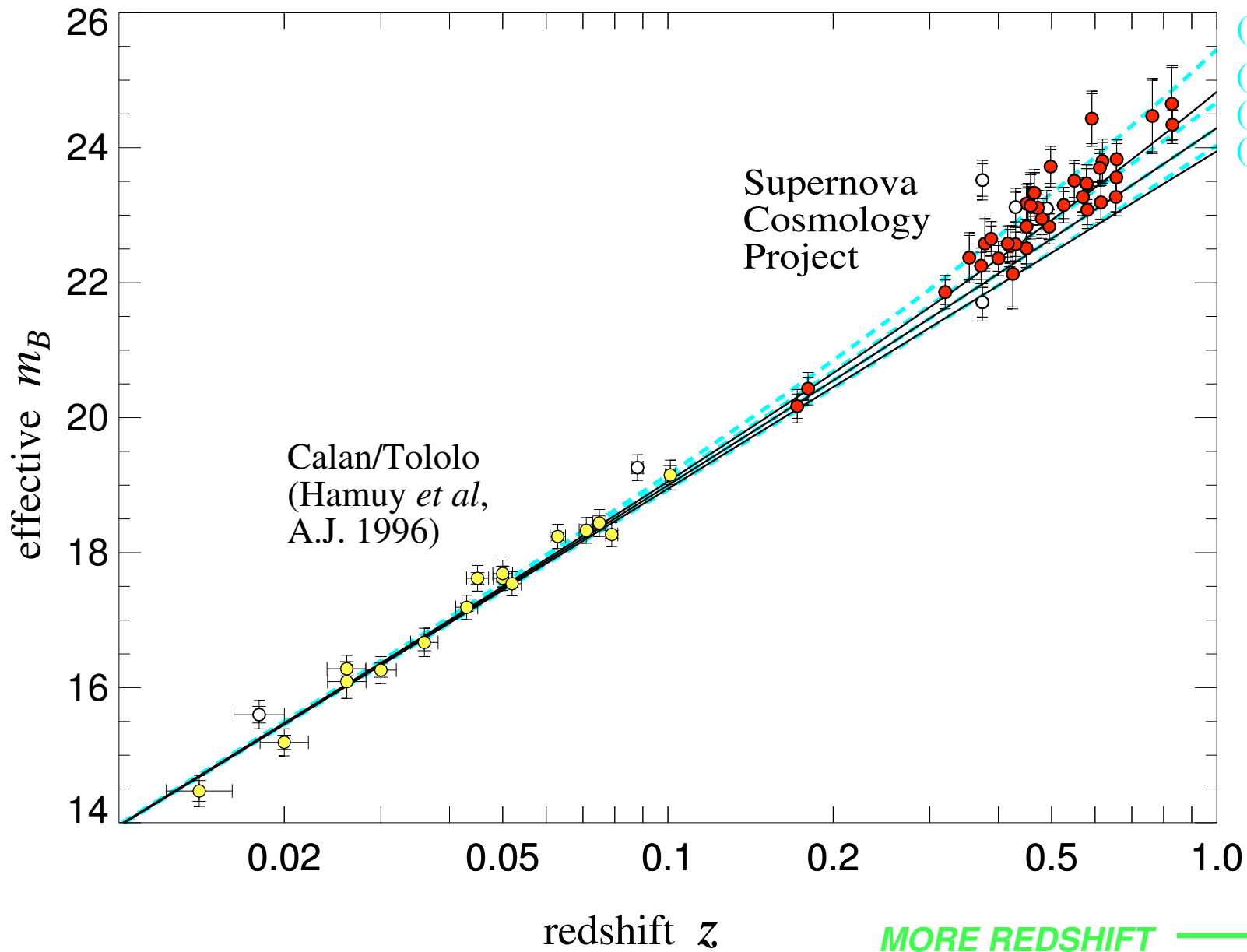
Therefore :  $v \uparrow \iff R \uparrow$  **Acceleration!**

Dark Energy:  $\rho$  drops slower than  $\frac{1}{R^2}$

i.e.  $\rho \propto R^{-3(1+w)}$  with  $w < -1/3$



Perlmutter, *et al.* (1998)

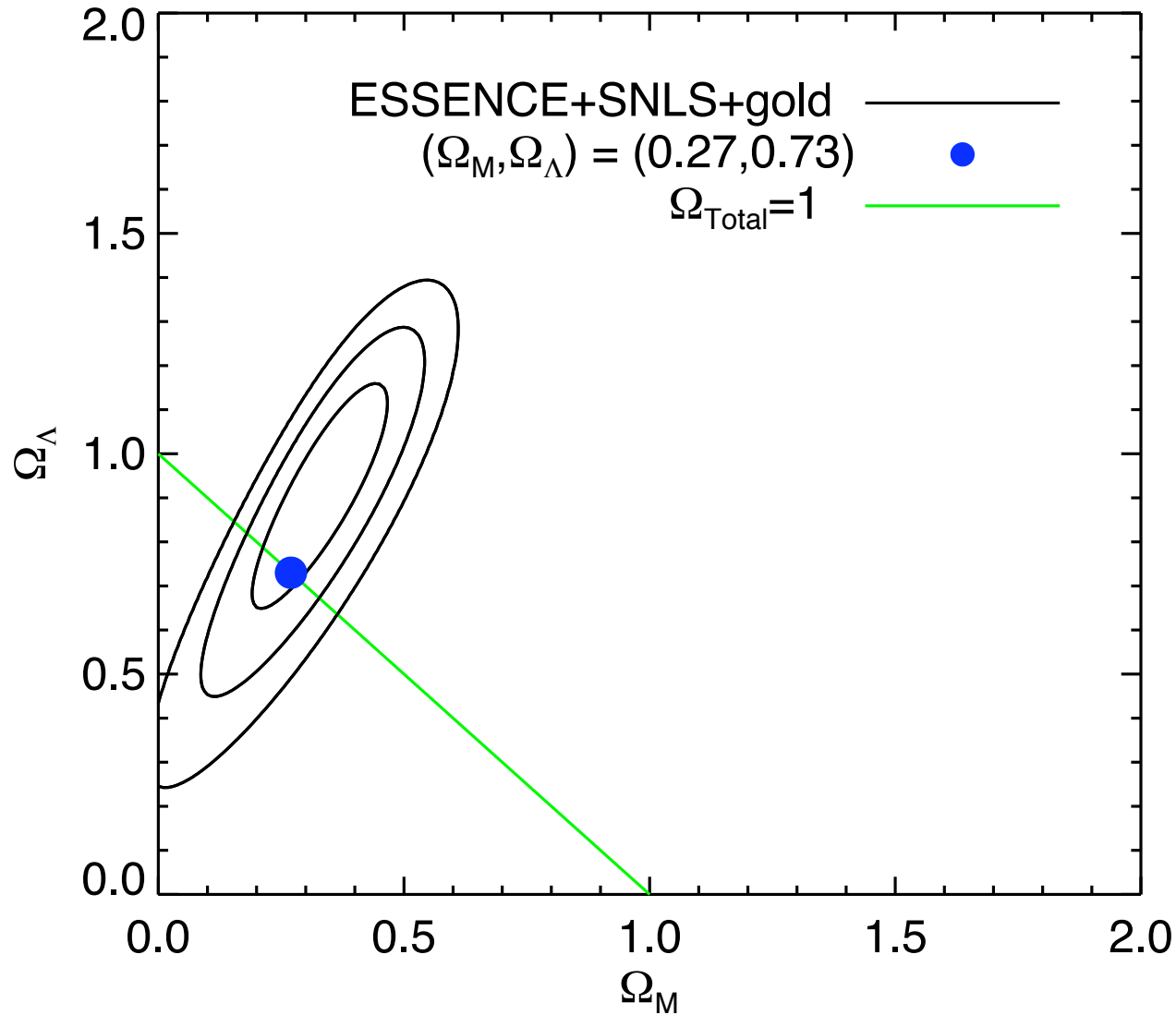


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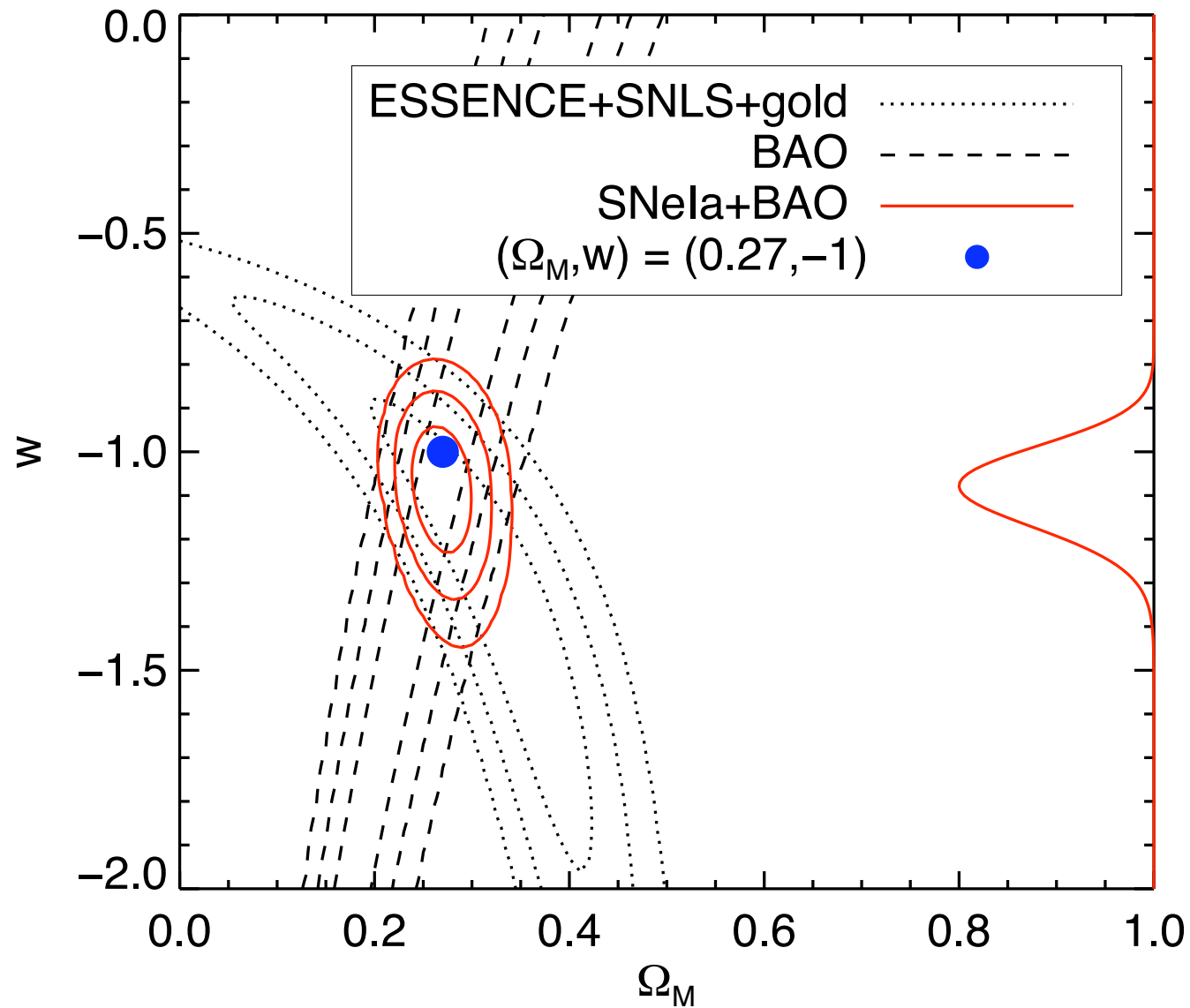
See also Riess *et al.* 98





70% dark energy, 30% matter





Dark energy  $\rho \propto R^{-0.6}$  to  $R^{1.2}$



What is dark energy?

1. Vacuum energy

(Einstein's cosmological constant)

2. Scalar field (Bose Einstein condensate)

3. Modified gravity (Einstein was wrong!)



# What is dark energy?

1. Vacuum energy

(Einstein's cosmological constant)

Observed value too small.

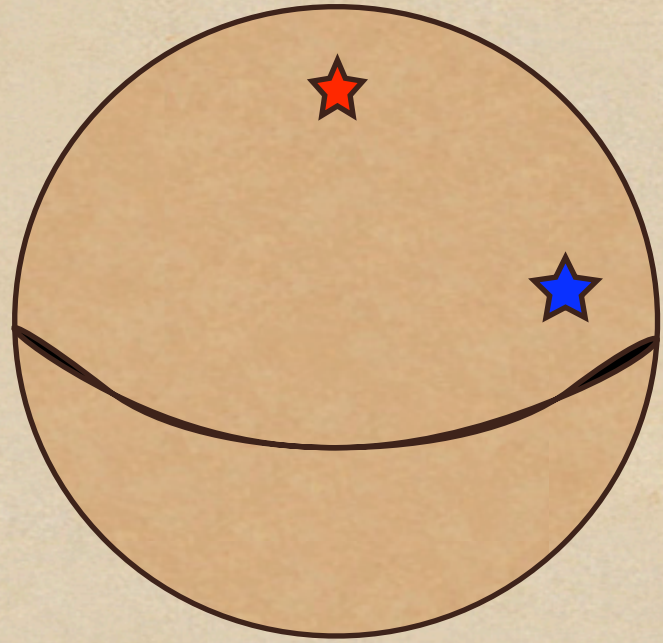
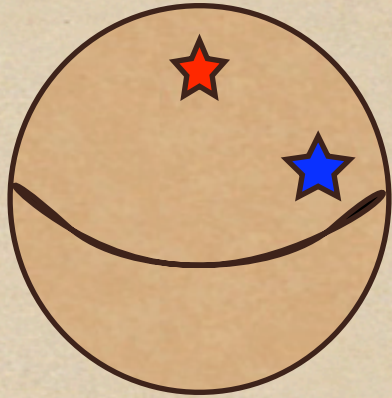
2. Scalar field (Bose Einstein condensate)

Required mass too small.

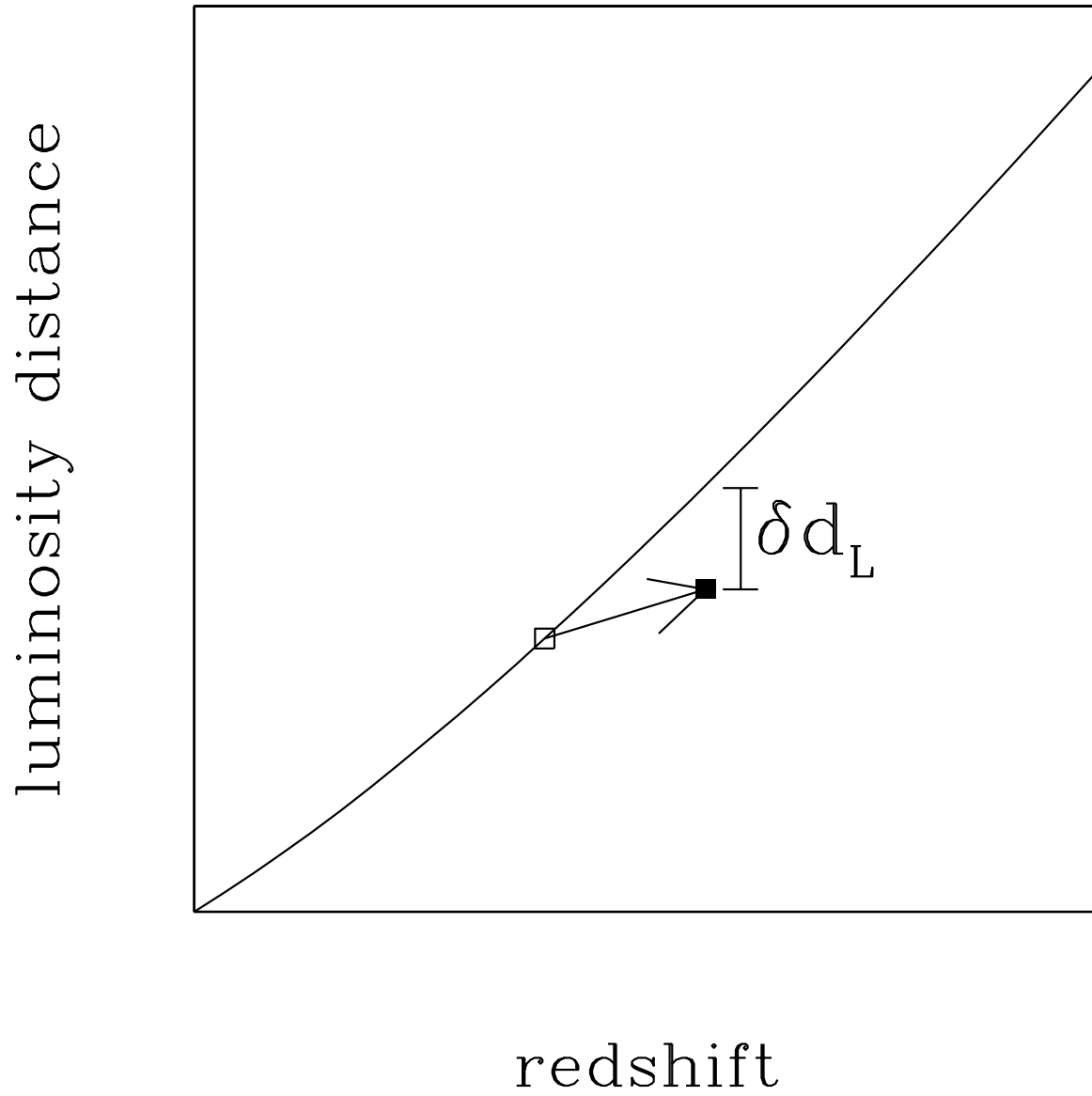
3. Modified gravity (Einstein was wrong!)

No compelling theory.

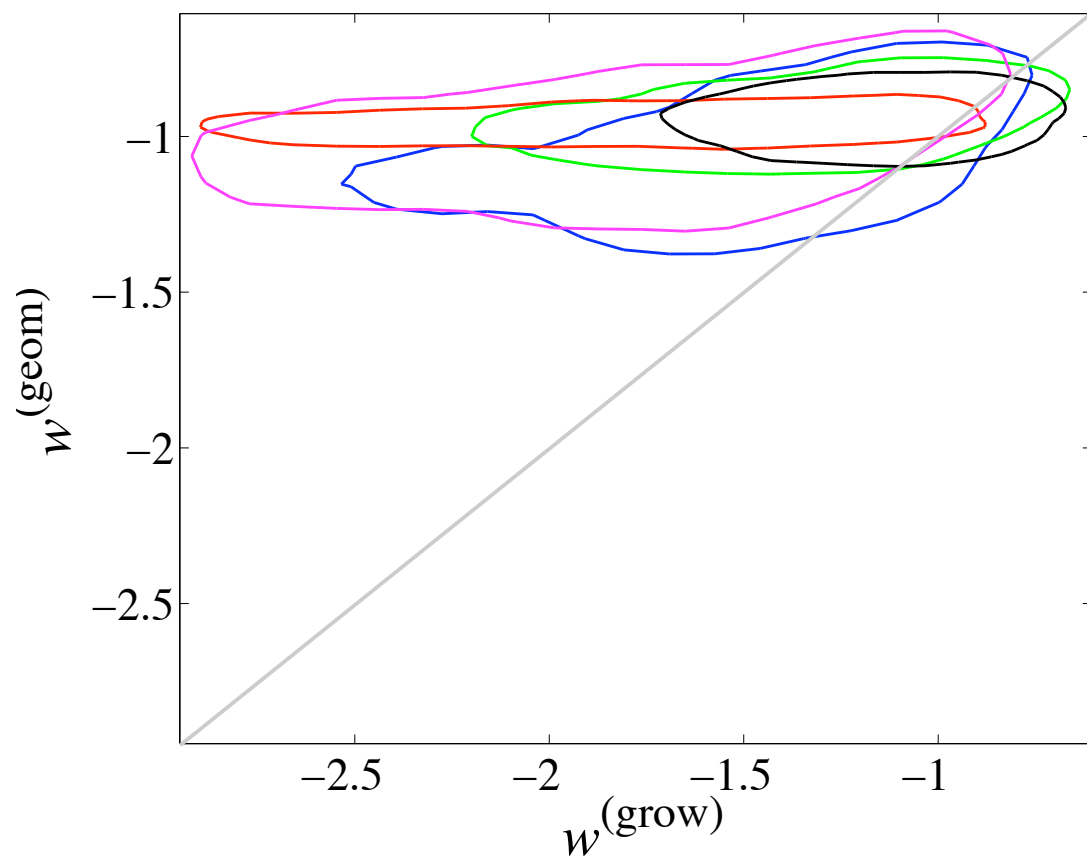
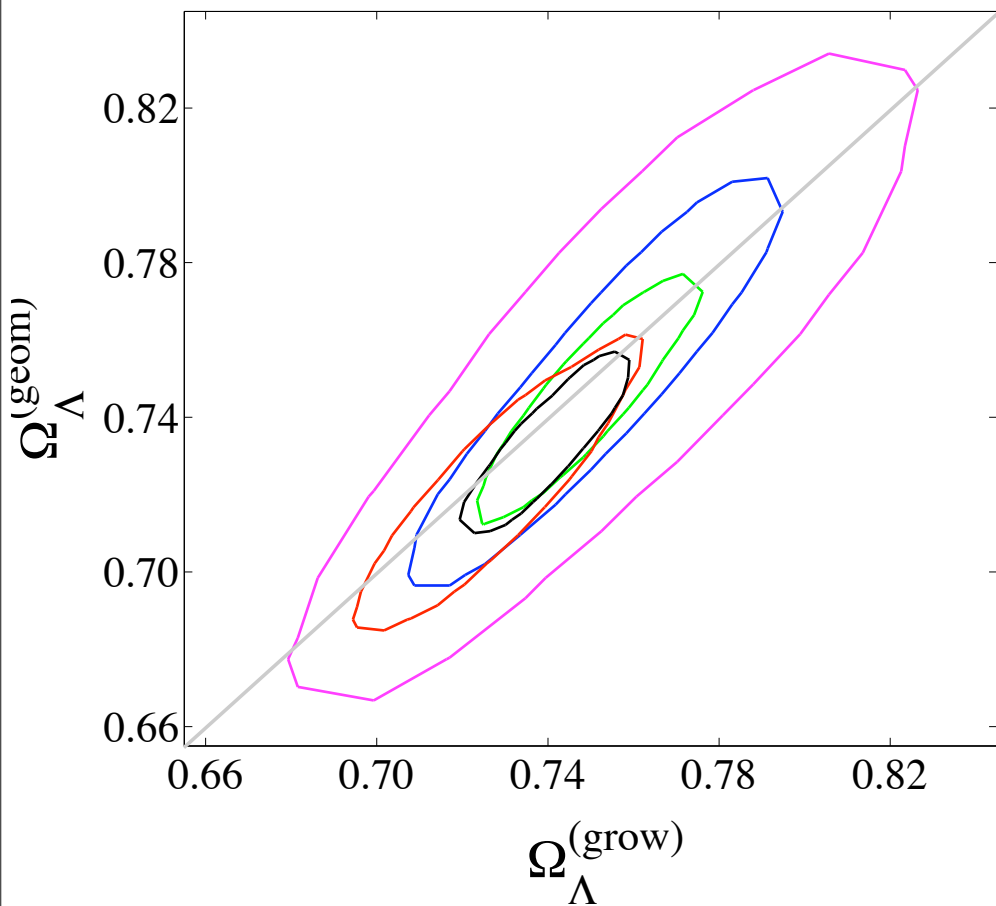












Wang, LH, May & Haïman 07

See also Li & Chu, Li, Chan & Chu 06



## Summary

- Basic concepts of a homogeneous, isotropic and expanding universe.
- Surprisingly, our current expansion appears to be accelerating. Explaining it, and measuring it precisely, is a major goal of cosmology today.







Let there be light.

Genesis 1:3