

X-RAY SPECTROSCOPY in ASTROPHYSICS

1

General literature

1. P. McWhirter : in "Plasma Diagnostic Techniques," Huddleston & Leonard (Eds.), 1965
2. S.M. Kahn & D.A. Liedahl : in "Physics with Multiply Charged Ions", Liesen, D. (Ed.), Plenum Press (1995) [simple intro]
3. R. Mewe : "Atomic Physics of Hot Plasmas" in : "X-ray Spectroscopy in Astrophysics", J. van Paradijs, J. Bleeker (Eds.), Springer, 1998 [collisional plasmas]
4. D.A. Liedahl : "Spectral Properties of PIE and NE Plasmas", in : "X-ray Spectroscopy in Astrophysics", J. van Paradijs, J. Bleeker (Eds.), Springer 1998 [radiation dominated & transient plasmas]
5. S.M. Kahn: lectures at recent Saas-Fee school (not yet, or unpublished)

Preliminaries:

2

TREMENDOUS progress since launch of
Chandra & XMM!

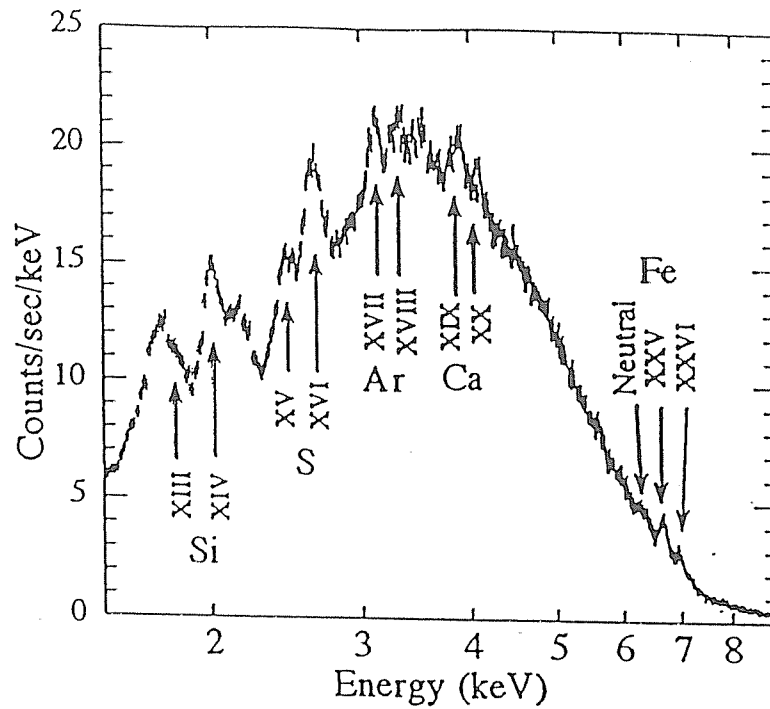


Fig. 1. Energy spectrum of Cyg X-3 obtained by SIS.
Identifications for prominent lines are also indicated
by arrows.

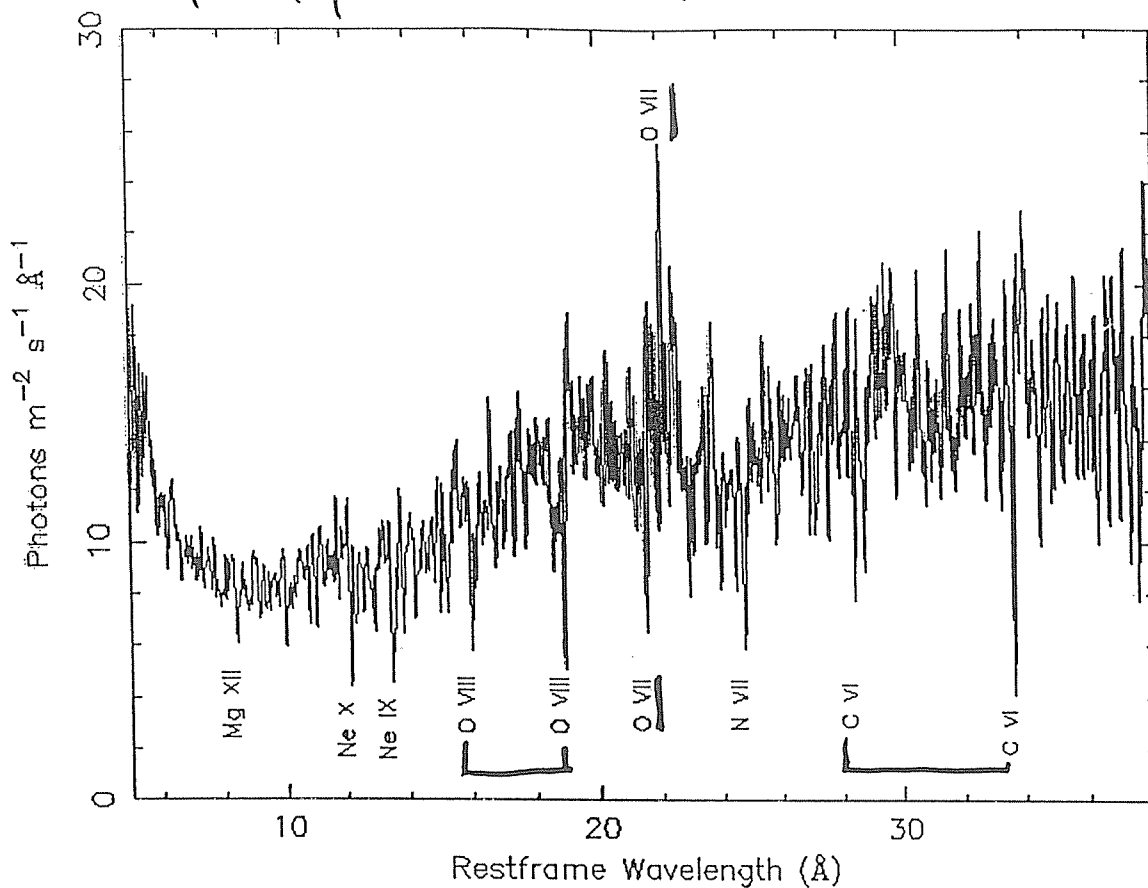
Ex: CCD spectrum of massive binary

[BH/NS + WR star] Cyg X-3

(Kitamoto & al., 1994, PASJ, 46, L105):

Recombination radiation from X-ray
photoionized wind of WR star

X-ray Absorption Line Spectrum of Seyfert 1 Galaxy NGC 5548



Chandra LETGS, Kaastra & al., 2000 :

- 1 deepest dips in noisy spectrum :
each coincides with strongest resonance
transition $n=1-2$ in H, He-like
C, N, O, Ne, Mg
 - 2 Absorption from every ion that should
be there IS in fact detected
- ⇒ powerful principle:
SPECTROSCOPIC CONSISTENCY

Approximate Energies of Interest.

5.

1. Nothing replaces the Bohr atom!

$$E_{nm} = Z^2 \cdot Ry \left(\frac{1}{n^2} - \frac{1}{m^2} \right) \quad ; Ry = 13.6 \text{ eV}$$

a) one-electron ions, resonance transitions (low densities \rightarrow no population in excited states):

$$E_{1m} = Z^2 \cdot Ry \left(1 - \frac{1}{m^2} \right)$$

| | | |
|------------------|----------------------|------------------------------|
| C VI Ly α | $E = 367 \text{ eV}$ | $\lambda = 33.8 \text{ \AA}$ |
| N | 500 | 24.8 |
| O | 653 | 19.0 |
| Ne | 1020 | 12.16 |
| Mg | 1469 | 8.44 |
| Si | 2000 | 6.20 |
| ... | | |
| Fe | 6895 | 1.80 |

$$\left(E = hc/\lambda \rightarrow E = 12.3985/\lambda, \quad \begin{array}{l} E : \text{keV} \\ \lambda : \text{\AA} \end{array} \right)$$

\Rightarrow abundant elements:
 $\approx 350 \rightarrow 2000 \text{ eV}$

Accurate transition Energies:

6.

Dirac Equation

(cf. Bethe & Salpeter: "QM of one and two electron atoms"; Sakurai: "Advanced QM")

Simple order of magnitude estimate:
relativistic corrections to energies:

$$E^2 = E_0^2 + p^2 c^2 \quad (E_0 \equiv mc^2)$$

$$\Rightarrow E \cong E_0 \left(1 + \frac{p^2 c^2}{2E_0^2} - \frac{1}{8} \left(\frac{p^2 c^2}{E_0^2} \right)^2 \right)$$

\Rightarrow successive orders of approximation

$$\text{smaller by } \sim p^2 c^2 / E_0^2 = \frac{Z^2 \alpha^2}{n^2}$$

\uparrow
(Bohr atom)

$$\Rightarrow \underline{Z^2 \alpha^2 = 1.9 \times 10^{-3} \text{ for C, already!}}$$

One-electron ions [cont'd]:

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Also: l, s degeneracy lifted

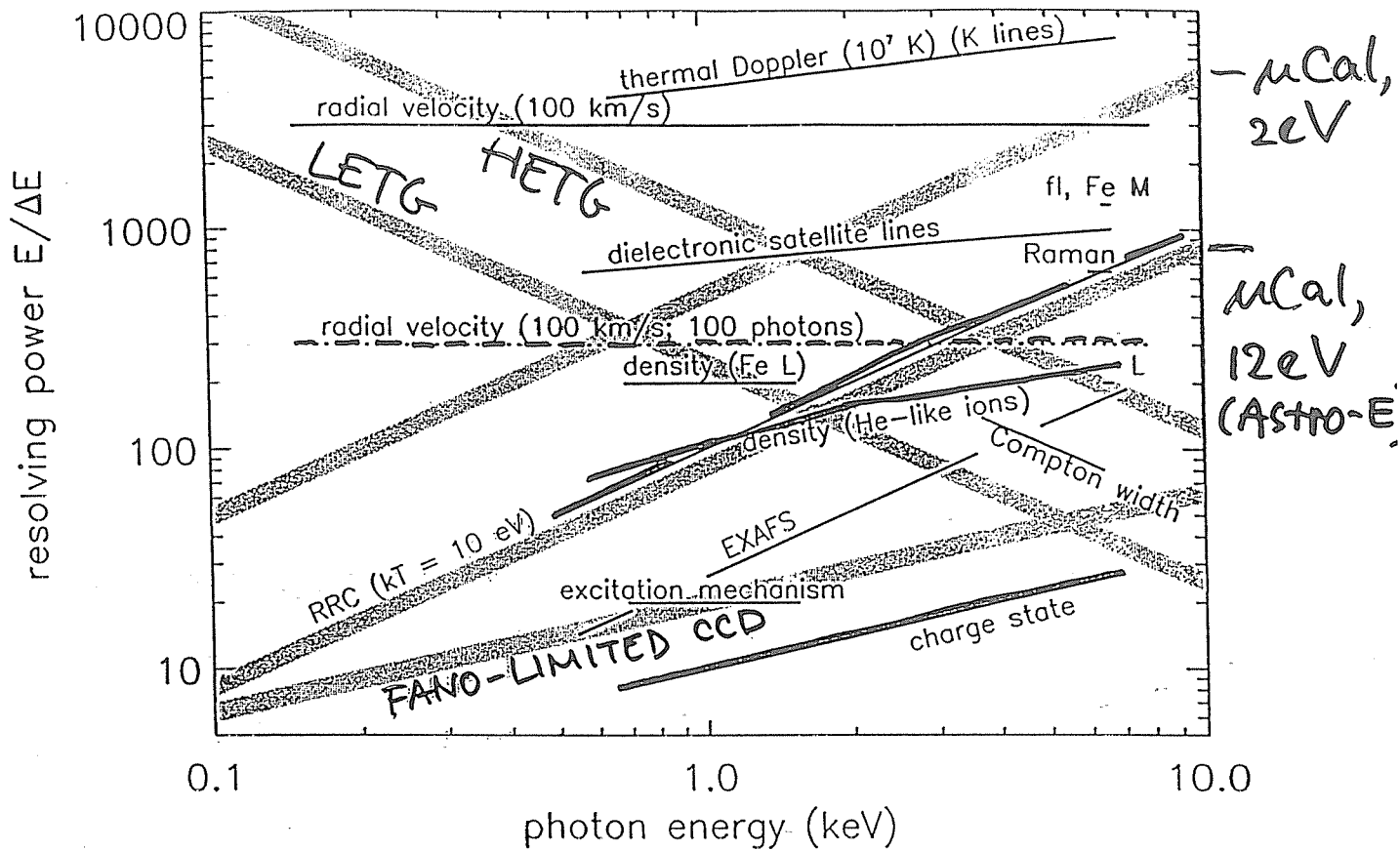
→ see "H β " in Fe XXVI in
Cygnus X-3!

Useful numbers for Ly-series:

- use solution to Dirac equation for H-like ions
- Tables compiled by Masao Sako
(masao@astro.columbia.edu;
masao@astro.caltech.edu after Sep 1, 2001)

Different Types of Spectrometer

(a sales pitch for gratings)



① Ionization detectors (prop counters, CCD's) :

natural energy scale : ionization energy

$\Rightarrow \Delta E \propto E^{1/2}$

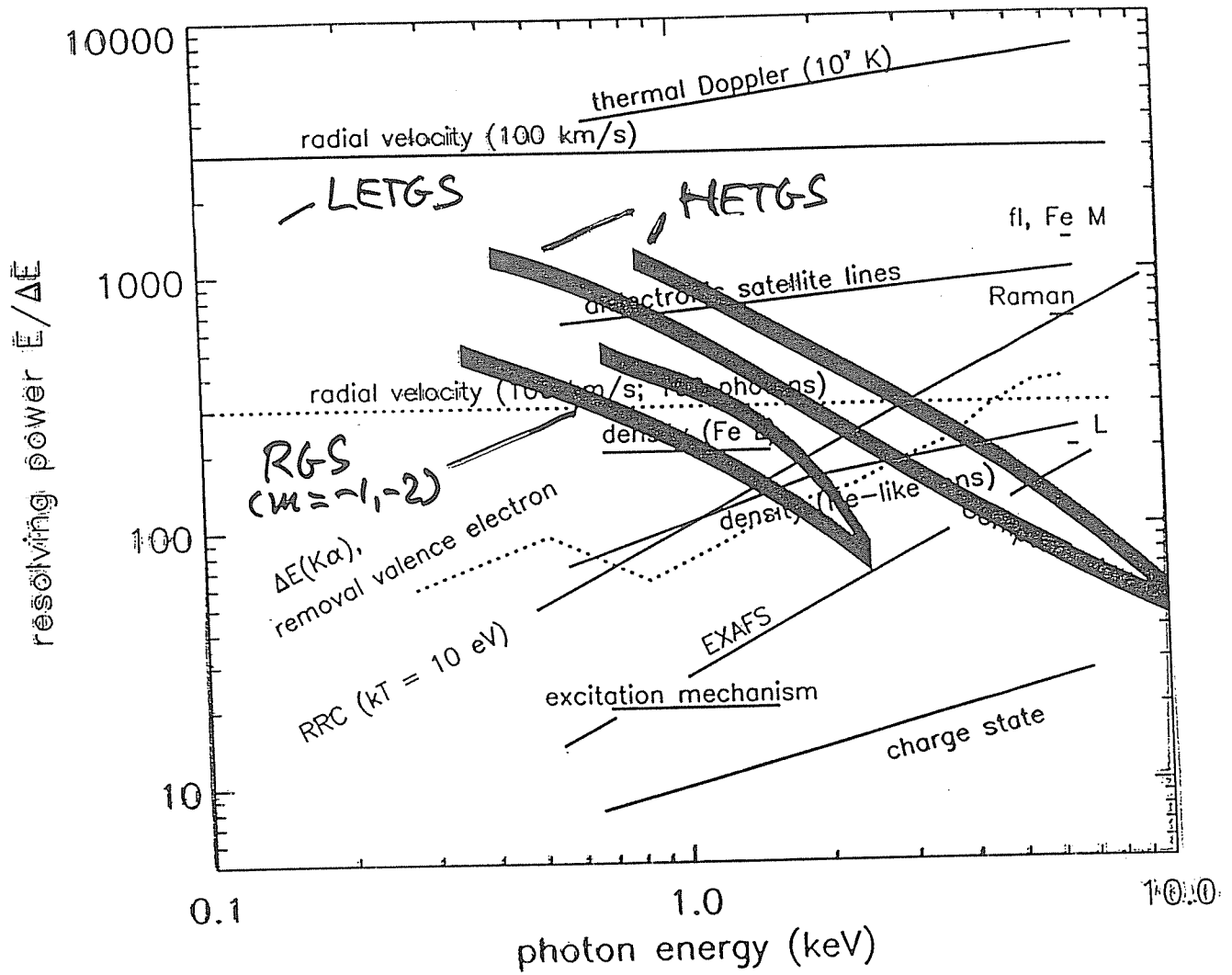
② Microcalorimeters : $\Delta E = \text{constant}$
(Quantum physics of lattice heat capacity)

③ Grating Spectrometers : $\Delta \lambda \approx \text{constant}$
(no fundamental limit)

\Rightarrow Gratings always beat CCD's, microcalorimeters at low energies!

Real Resolving Powers :

Diffraction Grating Spectrometers on Chandra, XMM-Newton



Chandra

- Telescope $\Delta\theta \lesssim 1''$

- transmission gratings:

$$R = \frac{\lambda}{\Delta\lambda} = \frac{\theta}{\Delta\theta}$$

R large because $\Delta\theta$ small

- $R \gtrsim 1000$

- $A_{\text{eff}} (E \lesssim 2 \text{ keV})$
 $< 100 \text{ cm}^2$
($\rightarrow 10 \text{ cm}^2$)

- Superior performance at $E > 2 \text{ keV}$

- resolution degrades
 $\Delta\varphi \gtrsim 1 \text{ arcsec}$

- either imaging OR
imaging spectroscopy

XMM-Newton 10a

- $\Delta\theta \sim 8-10''$

- Reflection Gratings:

$$\Delta\lambda = \frac{d}{m} \sin\alpha \cdot \Delta\theta$$

grazing incidence

$$\Rightarrow \sin\alpha \sim 1/50$$

compensates for bigger $\Delta\theta$

- $R \gtrsim 500$
(300 at 15 \AA)

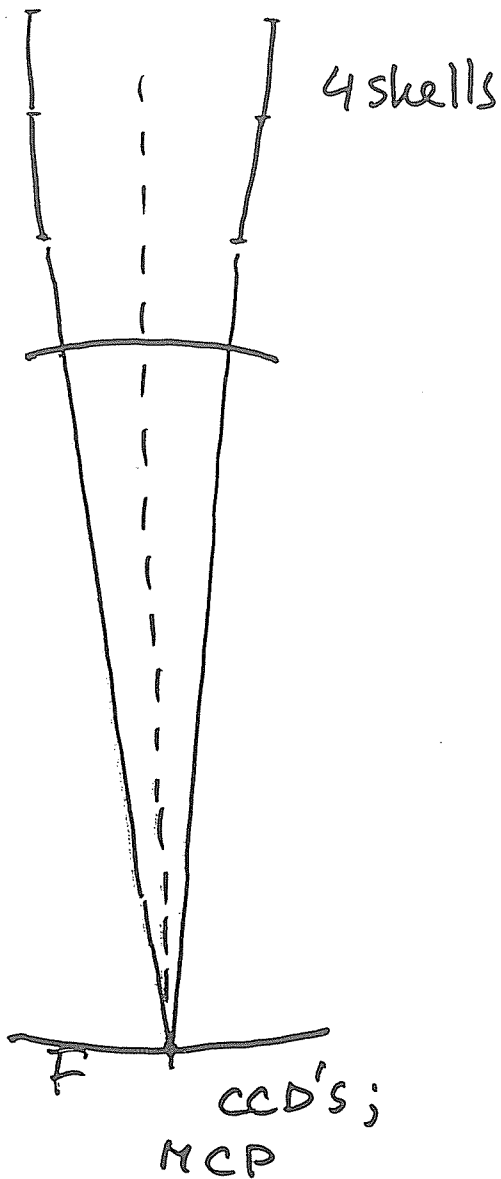
- $A_{\text{eff}} (E \leq 2 \text{ keV})$
 $\sim 100 \text{ cm}^2$

- band limited to $0.3 - 2.5 \text{ keV}$
($E > 2 \text{ keV}$: CCD's)

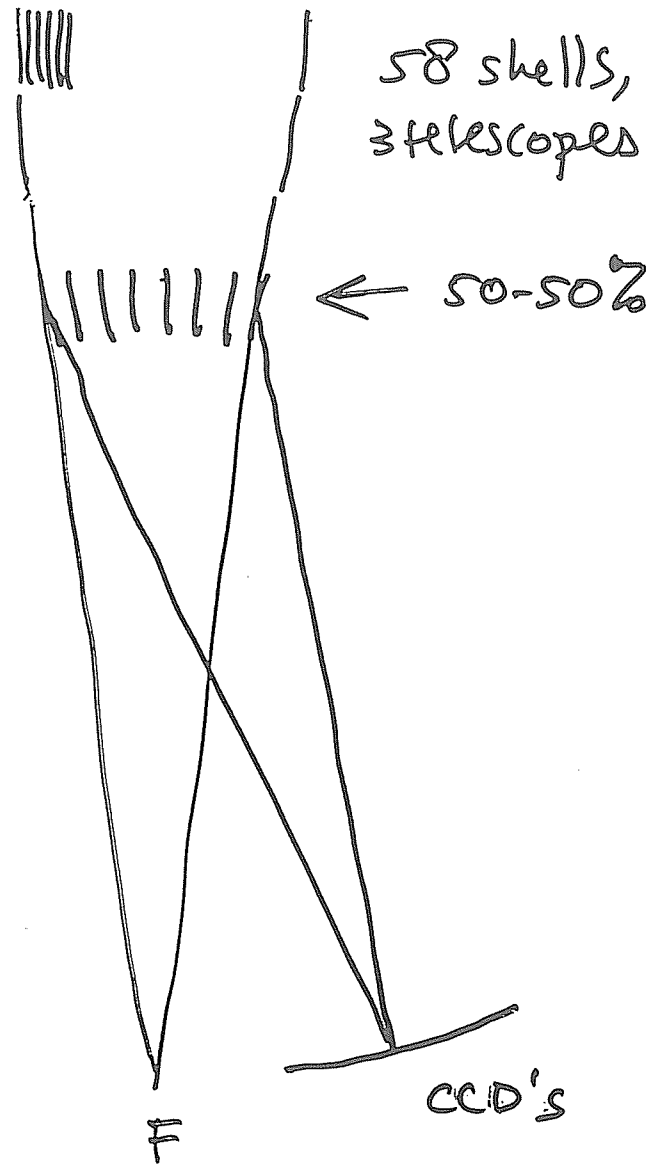
- resolution degrades
 $\Delta\varphi \gtrsim 30''$:
moderately extended sources.

- RGS always in
r.n. to the point in

Chandra



XMM-Newton 10⁶



Both "slitless" spectrometers:
spectral/spatial coupling along
dispersion direction

Discrete Transitions :

quick recapitulation

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- Atomic structure multi-electron systems:

$$H = H_{\text{central field}} + \text{electrostatic e-e} + \\ + \text{spin-orbit} + \dots$$

$$\equiv H_0 + H_{\text{pert}}$$

Electrostatic interactions:

$$\left. \begin{aligned} \sum \vec{l}_i &\equiv \vec{L} \\ \sum \vec{s}_i &\equiv \vec{S} \end{aligned} \right\} \text{ conserved}$$

$\Rightarrow L, S$ good quantum numbers

(non-relativistic,
electrostatic interactions only!)

Labeling:

$${}^{2S+1}L_J$$

$L = 0, 1, 2, \dots$: "S, P, D, F, ..."

e.g. (simplest example):

$$L \text{ in } \dots \text{ } 2P$$

Radiative Transitions:

Semiclassical (EM field classical);

First-order perturbation theory:

transition probability $i \rightarrow f$:

$$\propto |\langle f | H_{fi} | i \rangle|^2$$

H_{fi} induces the transition (interaction energy):

$$H_i = \frac{1}{2m} (\vec{p}_i - \frac{e}{c} \vec{A}) + e\varphi =$$

$$= \frac{p_i^2}{2m} + e\varphi - \frac{e}{mc} \vec{A} \cdot \vec{p}_i + \frac{e^2 A^2}{2mc^2}$$

↑
one photon

↑
two photon

Set $\vec{A}(\vec{r}, t) = \vec{A}(t) e^{i\vec{k} \cdot \vec{r}}$ (plane wave)

$$\Rightarrow H_{fi} = \vec{A}(\omega_{fi}) \frac{ie\hbar}{mc} \langle f | e^{i\vec{k} \cdot \vec{r}} \sum_i \nabla_i | i \rangle$$

↑
electron momenta

Dipole Approximation:

$$e^{i\vec{k}\cdot\vec{r}} = 1 + i\vec{k}\cdot\vec{r} + \frac{1}{2}(i\vec{k}\cdot\vec{r})^2 + \dots$$

↑
dipole approximation

because $|H_{fi}|^2 \propto |d_{fi}|^2$

Higher order terms smaller by

$$\vec{k}\cdot\vec{r} \sim ka_0$$

$$\sim \frac{\text{size atom}}{\text{radiation wavelength}}$$

$$\sim Z\alpha$$

$$\sim v/c \ll 1 \text{ in}$$

dipole approximation

(and probability $\propto |\vec{k}\cdot\vec{r}|^2$)

Nomenclature:

Electric Dipole, E1, "dipole allowed"

- { Electric Quadrupole (E2),
- { Magnetic Dipole (M1),
- Electric Octupole

Spontaneous Transition Rate A_{ji}

(from induced rate & relation A, B) :

$$A_{ji} = 6.7 \times 10^{15} \frac{\omega_i}{\omega_j} f_{ij} Z_A^{-2}$$

$f_{ij} \sim 1$, constant

$$\Rightarrow \underline{A_{ij} \propto Z^4}$$

- Symmetry properties of $\langle f | e^{i\vec{k}\cdot\vec{r}} \nabla_i | i \rangle$ give rise to selection rules.

E1 transitions :

$$\Delta L = 0, \pm 1$$

$$\Delta S = 0$$

$$\Delta J = 0, \pm 1 ; \quad J=0 \rightarrow J=0$$

$$M_J=0 \rightarrow M_J=0$$

- Other Processes (e.g. collisions with charged particles) : same idea.

Example : "spin-flip" transitions 15

"proton spin-flip" in superstrong \vec{B} -field

● $B \sim 10^{15}$ G (so-called "magnetar", strongly magnetized young NS)

● circular orbits charged particles in \vec{B} -field quantized ("Landau levels"):

$$E_n = (n + \frac{1}{2}) \hbar \omega_B =$$

$$= (n + \frac{1}{2}) \hbar \frac{qB}{m_p c} \Rightarrow$$

$$\Delta E = 6.3 (B / 10^{15} \text{ G}) \text{ keV}$$

● $\frac{\text{probability spin flip}}{\text{probability } \Delta n = 1} \sim \left(\frac{v}{c}\right)^2$

$$\sim \frac{\Delta E}{m_p c^2} = \frac{6.3 B_{15}}{511 \times 1836} \ll 1$$

→ very weak transition

Example: He-like ions $n = 1-2$

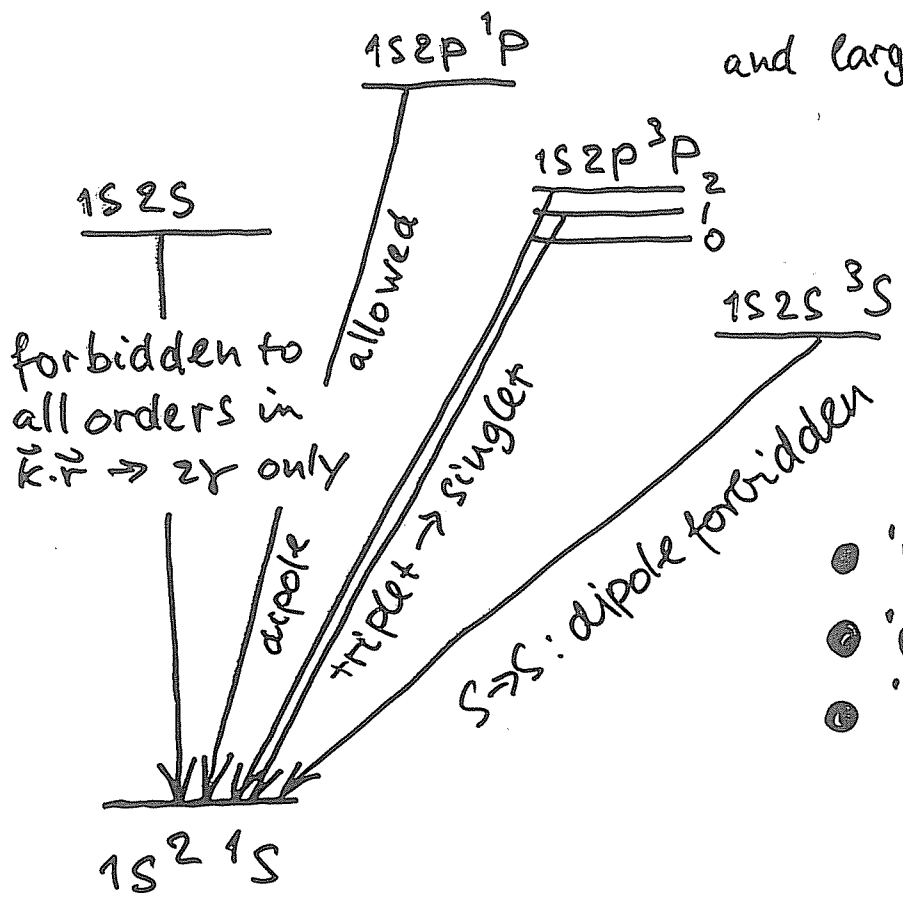
two electrons: eigenfunctions of $|\vec{S}_{total}|^2$:

$\uparrow\uparrow, \downarrow\downarrow, \uparrow\downarrow + \downarrow\uparrow$: triplet

$\uparrow\downarrow - \downarrow\uparrow$: singlet

total wavefunction must be antisymmetric

spin anti \rightarrow space symmetric
 \leftarrow Pauli: e's close, $\Delta E_{electrostatic} > 0$
 and larger than triplet states



- 'resonance' w
- 'intercombination' x, y
- 'forbidden' z

He-like ions are IMPORTANT in X-ray astronomy!

Astrophysical Plasmas

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- low density ; high ionization
- optically thin (ignore radiative transfer)
- (● $f(v)$ Maxwellian)

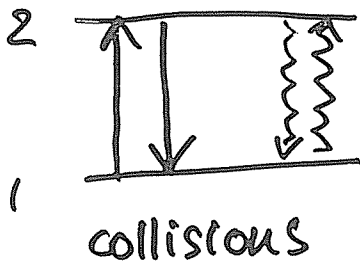
⇒ radiation excited in source escapes freely ;
spectrum directly reflects physical conditions at the source

(velocities, density, temperature, ionization balance, degree of equilibration,)

- examples : hot gas stellar coronae, SNR, ISM, clusters, IGM ; highly ionized gas in accretion flows, GRB Afterglows (?),

- what is 'low' density ?

spontaneous decay



collisional \downarrow rate \gg

spontaneous decay rate :

⇒ MEDIUM in LTE : thermal energy / radiation field very

(i.e. continuous conversion

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thermal energy gas \rightleftharpoons radiation)

[NB: if radiative transitions dominate,
 \Rightarrow TE if $I_{12} \rightarrow B_{12}(T)$, i.e. if $\tau_{12} \gg 1$]

n "low" if

$$A_{21} \gg n_e C_{21}(T_e)$$

$$\Rightarrow n_e \gtrsim 1.4 \times 10^{15} (Z+1)^6 T^{1/2} \text{ cm}^{-3}$$

● If n_e "low":

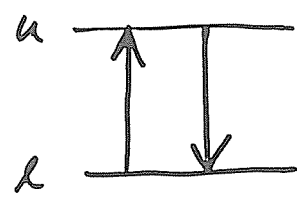
- most ions in $n=1$
- excitations followed by production of photon
- ionization balance \neq Saha, but found from rate equations

(sometimes referred to as "coronal approx.", but also applies to low density radiation dominated plasma's)

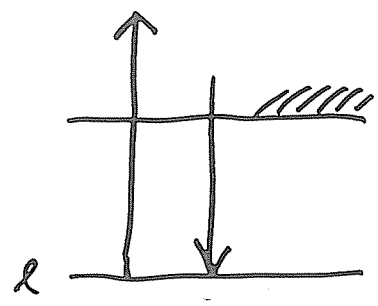
Most Common Interactions between electrons, ions, and photons:

1. Compton scattering on free or bound e^- 's

2.

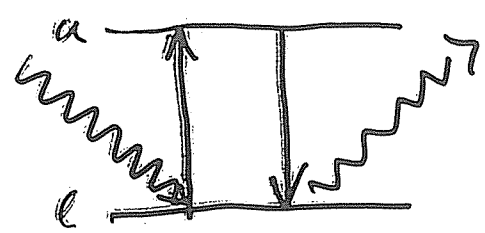


collisional excitation/
deexcitation

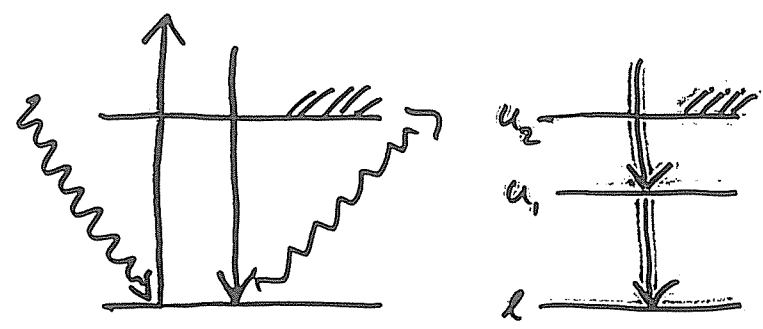


collisional ionization/
3-body recombination
($1e^-: f \rightarrow f, 1e^-: f \rightarrow b$;
plus ion)
3BR only at high
densities!

3.



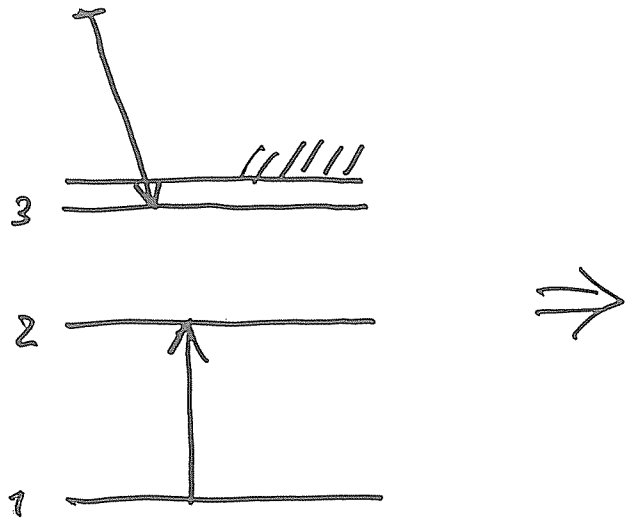
photoexcitation;
(photon can be line or
continuum); radiative
decay.



photoionization;
radiative
recombination; "cascade"

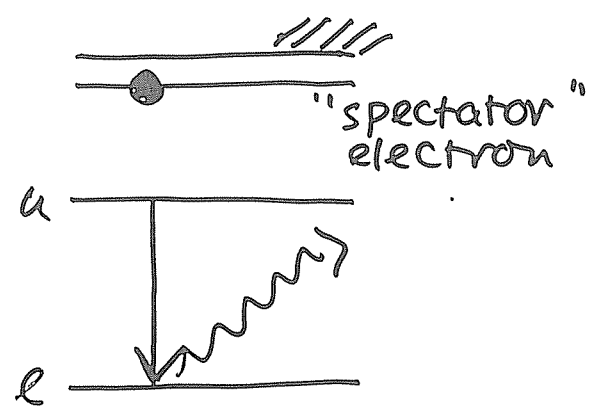
If $l=1, u=2$: "resonance line" $u=1-2$;
photon can not be destroyed & scatters

4.



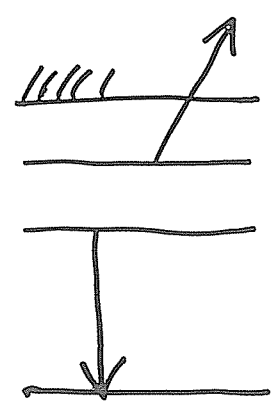
dielectronic recombination

(if "3" in continuum:
"resonant excitation")



"satellite line"
(close to $u \rightarrow l$
in ion $Z+1$)

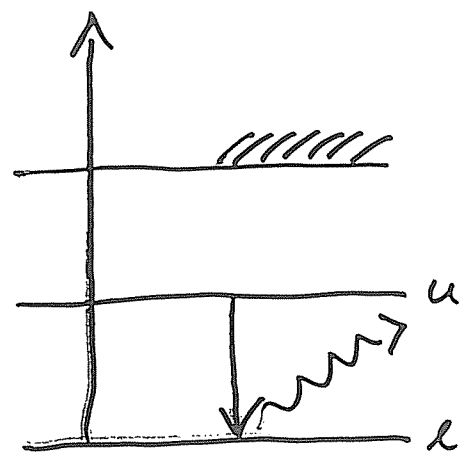
OR



Auger ionization

(either CI or PI)

5.



fluorescence

$$y \approx (Z/26)^4 \times 0.3$$

or Auger ; no
photons, only
electrons

Cross-sections:
cf. compilation in
Mewe (1998)

4. IONIZATION BALANCE.

21.

Roughly speaking, two types of high ionization plasma:

$$\left\{ \begin{array}{l} \text{collisionally ionized} : kT_e \sim \chi \\ \text{photoionized} : kT_e \ll \chi \end{array} \right.$$

(Mixed type, if radiation energy density high, and also $kT_e \sim \chi$).

4.1 collisionally ionized gas
c.a.k.a. "coronal plasma", or just: "hot gas")

- thermal balance:
heat in = radiation out
- ionization balance:

$$\begin{aligned} \frac{dn_i}{dt} = & +n_e n_{i-1} C_{i-1,i} + \\ & + n_e n_{i+1} \alpha_{i+1,i} - \\ & - n_e n_i (C_{i,i+1} + \alpha_{i,i-1}) \end{aligned}$$

Calculations:

- approximate expressions in Mewe ('98)
- calculations: Arnaud & Rothenflug, 1985, A&A Suppl., 60, 425
- Fe L: Arnaud & Raymond, 1992,

NB Auger ionization couples ions several stages apart! (not shown in dn_i/dt)

Balance is between direct collisional ionization, and RR + DR

↑
important at low T
due to resonant character
of process

➔ non-equilibrium ionization:

$$\frac{dn_i}{dt} \neq 0 \quad ;$$

$$\text{characteristic timescale: } \frac{1}{n_e \alpha}, \frac{1}{n_e C}$$

Approximate expressions:

$$n_e t_{\text{ion}} \approx 10^{10} (z+1)^4 n_z^{-4} \sum_z^{-1} T^{-1/2} e^{\gamma} \quad [\text{cm}^{-3} \text{s}]$$

↑
charge

↑

↑ nr. valence electrons

↑ principal quantum #
valence shell

$$\gamma \equiv 1.6 \times 10^5 (z+1)^2 n_z^{-2} T^{-1}$$

$$n_e t_{\text{rec}} \approx 10^{11} (z+1)^{-2} n_z^{5/2} \sum_z^{-1} T^{1/2} \quad [\text{cm}^{-3} \text{s}]$$

↑

↑ nr. holes in valence shell

(Mewe [1987])

Examples:

- He-like \rightarrow H-like O at $T = 5 \cdot 10^6$ K:

$$(n_e = 1, z = 6, \xi_z = 2, y = 1.6)$$

$$\rightarrow n_e t_{\text{ion}} \approx 2.6 \times 10^{10} \text{ cm}^{-3} \text{ s}$$

$$\text{ISM, } n_e \sim 1 : t_{\text{ion}} \sim 800 \text{ yrs!}$$

so SNR, $t < t_{\text{ion}}$: under ionized

- stripped \rightarrow H-like O at $T = 10^8$ K:

$$(\xi_z = 2, n_e = 1, z = 8)$$

$$\rightarrow n_e t_{\text{rec}} \approx 6 \cdot 10^{12} \text{ cm}^{-3} \text{ s}$$

GRB: afterglow-illuminated ejecta:

If you detect bound O 1 day after

the burst: $t_{\text{rec}} \lesssim 10^5 \text{ sec}$

$$\Rightarrow n_e \gtrsim 6 \cdot 10^7 \text{ cm}^{-3}$$

4.2 X-ray Photoionized Gas

24.

- energy balance :

photoelectric, Compton heating +
whatever else =
= radiative cooling

- ionization balance :

$$\frac{dn_i}{dt} = -n_i \int_{\chi}^{\infty} dE \sigma(E) \frac{F(E)}{E} + n_{i+1} n_e \alpha(T)$$

(only 2 stages shown)

- 1: thermal balance & ionization balance
COUPLED (through $\alpha(T_e)$) [UNLIKE
collisional plasma's]

explicit solutions: $\boxed{kT_e \ll \chi}$ COOL

(Kallman & McCray, 1982, ApJ Suppl. 50, 263)

\Rightarrow XSTAR code

Gary Ferland \Rightarrow CLOUDY

Hagai Netzer \Rightarrow ION ; & others)

- 2: degree of ionization scales with ξ :

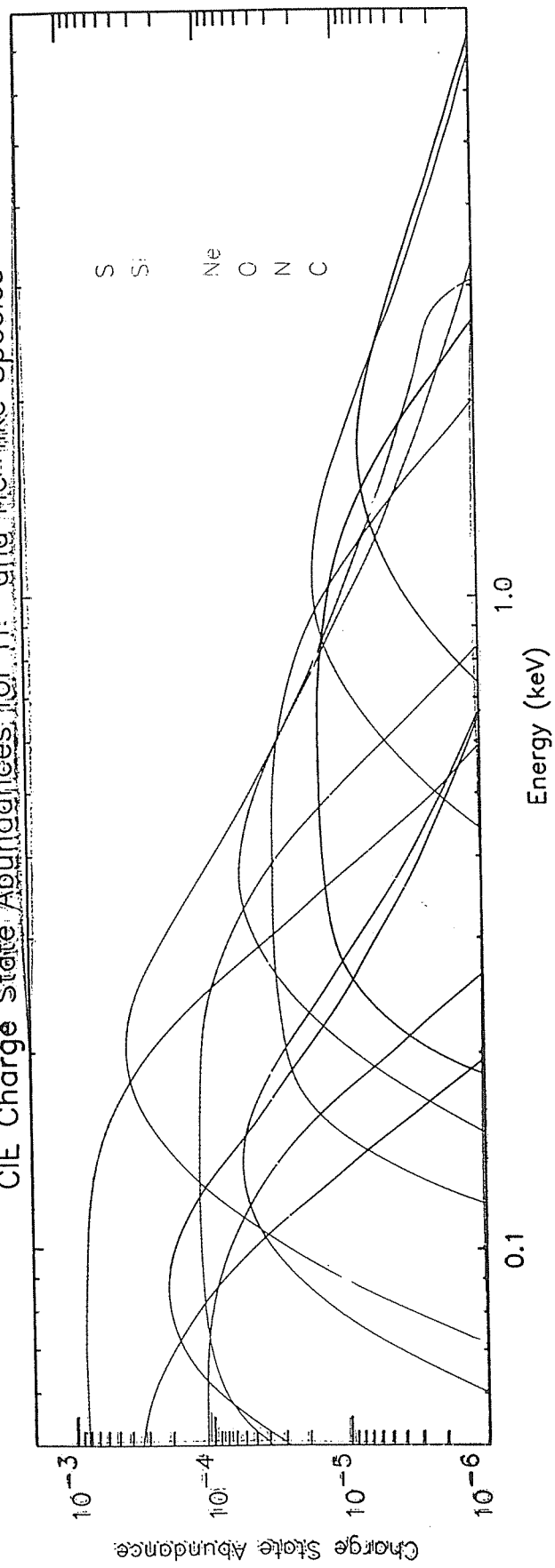
in equilibrium:

$$\frac{n_{i+1}}{n_i} = \boxed{\frac{L}{n_e r^2}} \times \frac{1}{4\pi} \frac{\int_{\chi}^{\infty} dE \sigma(E) f(E) \cdot E^{-1}}{\alpha(T_e)}$$

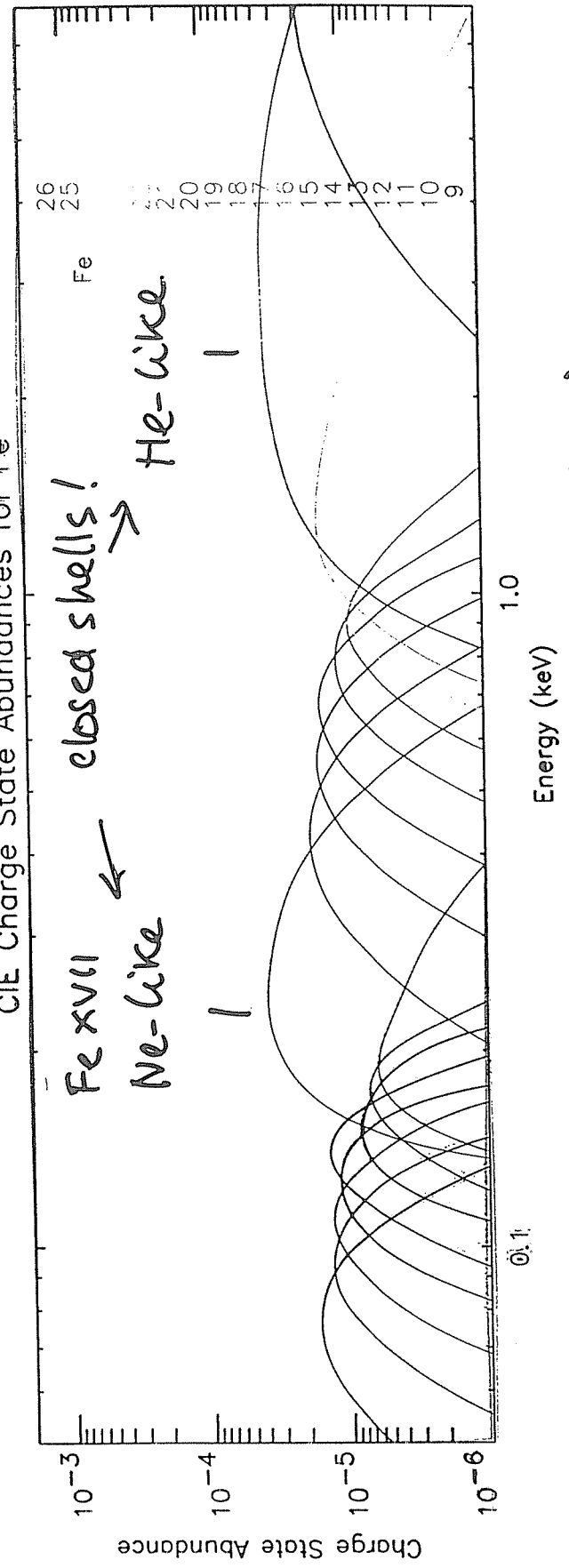
$= \xi$

COLLISIONAL IONIZATION EQUILIBRIUM

CIE Charge State Abundances for H- and He-like Species



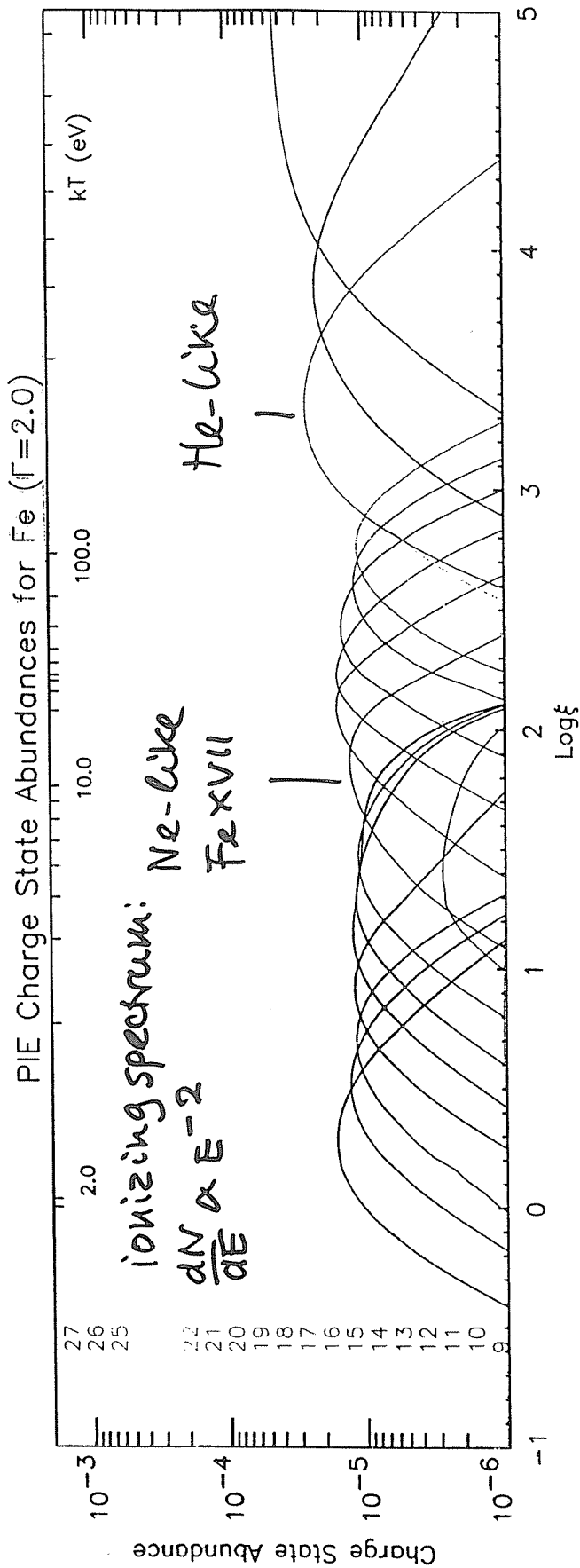
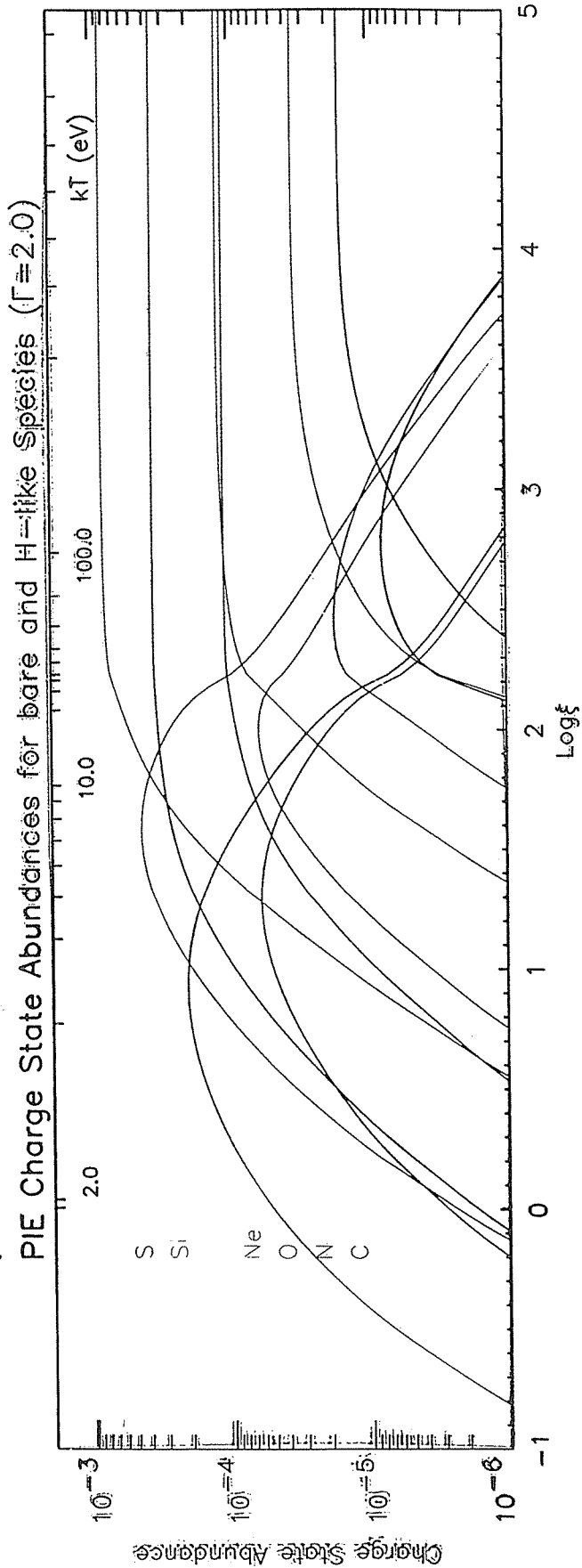
CIE Charge State Abundances for Fe



cie. electron temperature

Ref: Arnaud, M. and Rothenflug, R. 1985, A&AS, 60, 425

PHOTO IONIZATION EQUILIBRIUM



NB : ● collisional balance neatly
 sequential $n_i \rightarrow n_{i+1} \rightarrow n_{i+2}$
 $\xrightarrow{kT_e}$

● photoionization balance more messy:
 multiple species simultaneously present
 (consequence of "flat" ionizing spectrum
 E^{-2} , as opposed to $f(v)$ [Maxwell])

➔ Fe L ions cover wide range in either
 kT_e , ξ : excellent diagnostics over
 wide range in conditions

Fun calculation: fluorescence line
 fluxes for different elements:

$$\text{fluorescence rate} = n \cdot y \cdot \int_x^{\infty} dE \cdot F_0 E^{-\Gamma} \sigma(E)$$

$$\sigma(E) \cong 6 \cdot 10^{-18} Z^{-2} (\chi/E)^3 \text{ cm}^2 ;$$

set $\Gamma = 2$ (AGN, GRB afterglow)

$$\Rightarrow \text{rate} = n \cdot y \cdot F_0 \sigma_0 \cdot \frac{1}{4Z^2 \chi}$$

Now, $\chi \propto Z^2$, so rate $\propto \frac{y}{Z^4}$; and since

$y \propto Z^4 \Rightarrow \text{rate} = \text{independent of } Z!$

5. Collisional Plasma's: Spectroscopy

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1. Collisional excitation rate =
photon emission rate (in our case)

\propto ion abundance \times excitation rate
[Mewe '88]

\Rightarrow strongest dependence is in
ionization balance

\Rightarrow strongest T_e -diagnostic from ionization
balance (unfortunately - involves a
lot of explicit rate coefficients)

\Rightarrow emission spectra individual ions
NOT very sensitive to T_e , in T_e -range
where ion observable [ionization
balance!], except in unusual
circumstances

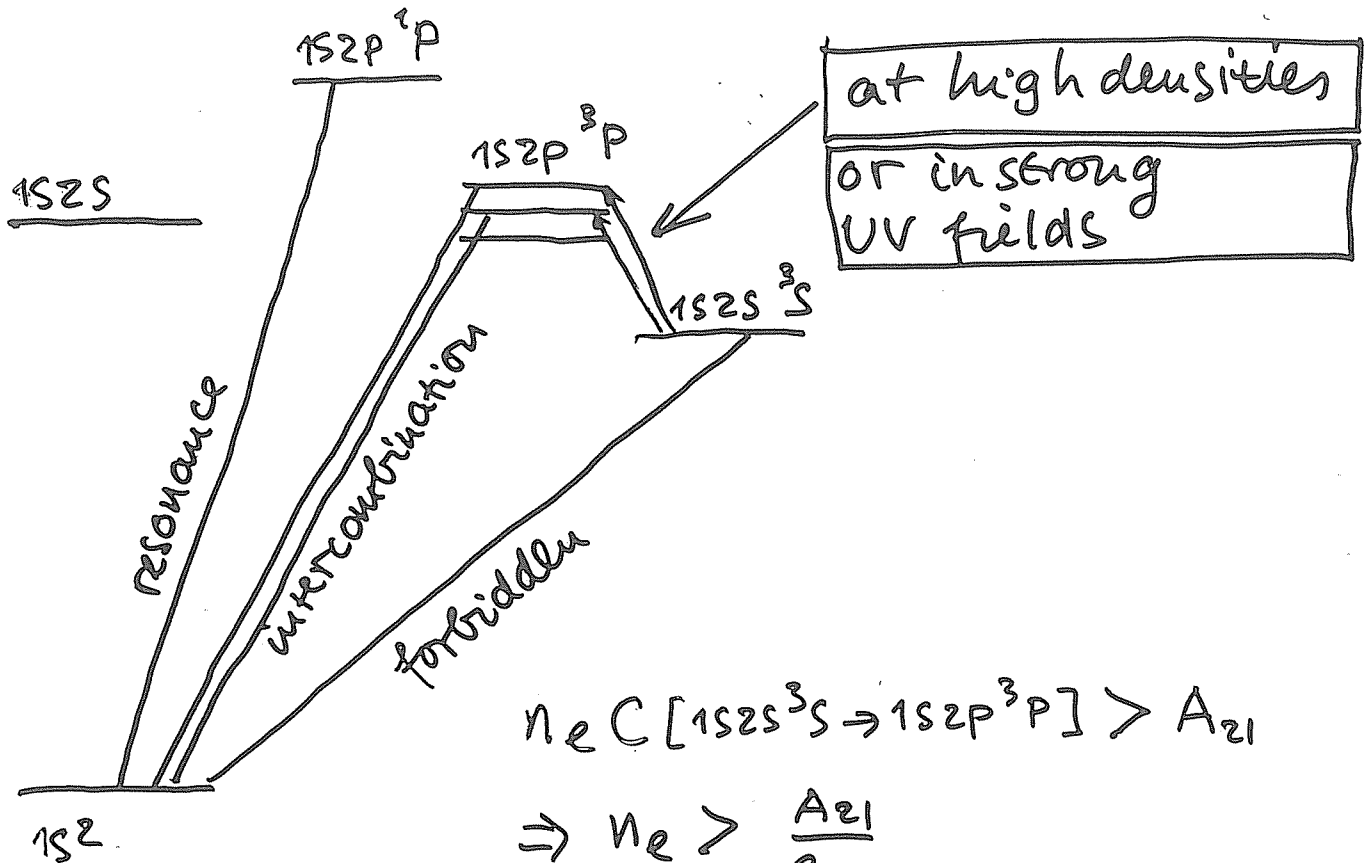
ex: He-like ions placed in very high
 T_e (compared to equilibrium
ionization balance):

emission line ratios sensitive at
high T_e . Cf. Andy Rasmussen et al.,
2001, A&A, 365)

2. Density sensitivity He-like

29.

$n = 1-2$ emission spectrum



$$n_e C[1s2s^3S \rightarrow 1s2p^3P] > A_{21}$$

$$\Rightarrow n_e > \frac{A_{21}}{C_{22}}$$

collisional transfer faster than spontaneous decay (easy, because A_{21} forbidden)

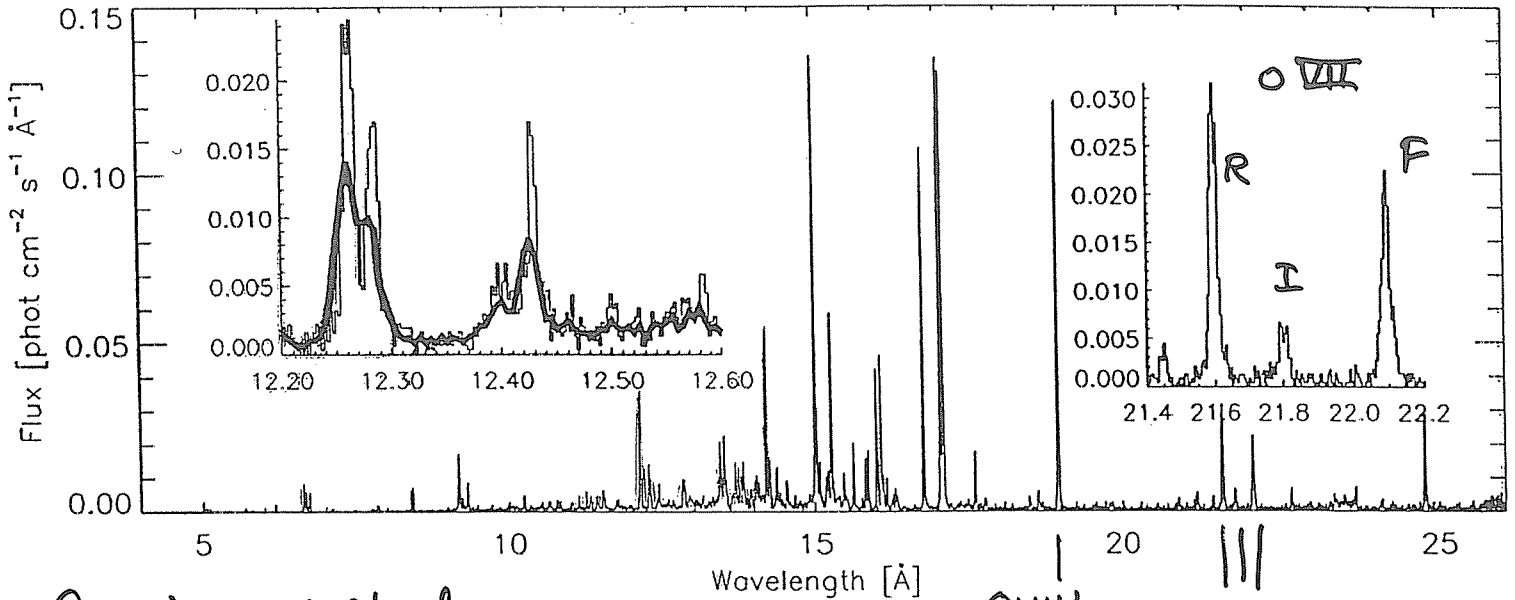
- $n_{e,crit}$ depends on Z ; ranges $\sim 10^8 - 10^{12} \text{ cm}^{-3}$
C - Si

- get upper limit if F strong; real measurement if $n_e \gtrsim n_{e,crit}$

- radiative transfer: O stars, accretion disks

Example: HETGS spectroscopy of coronae in Capella

Fe XVII 15.014, 15.26,
16.78, 17.05, 17.10 Å



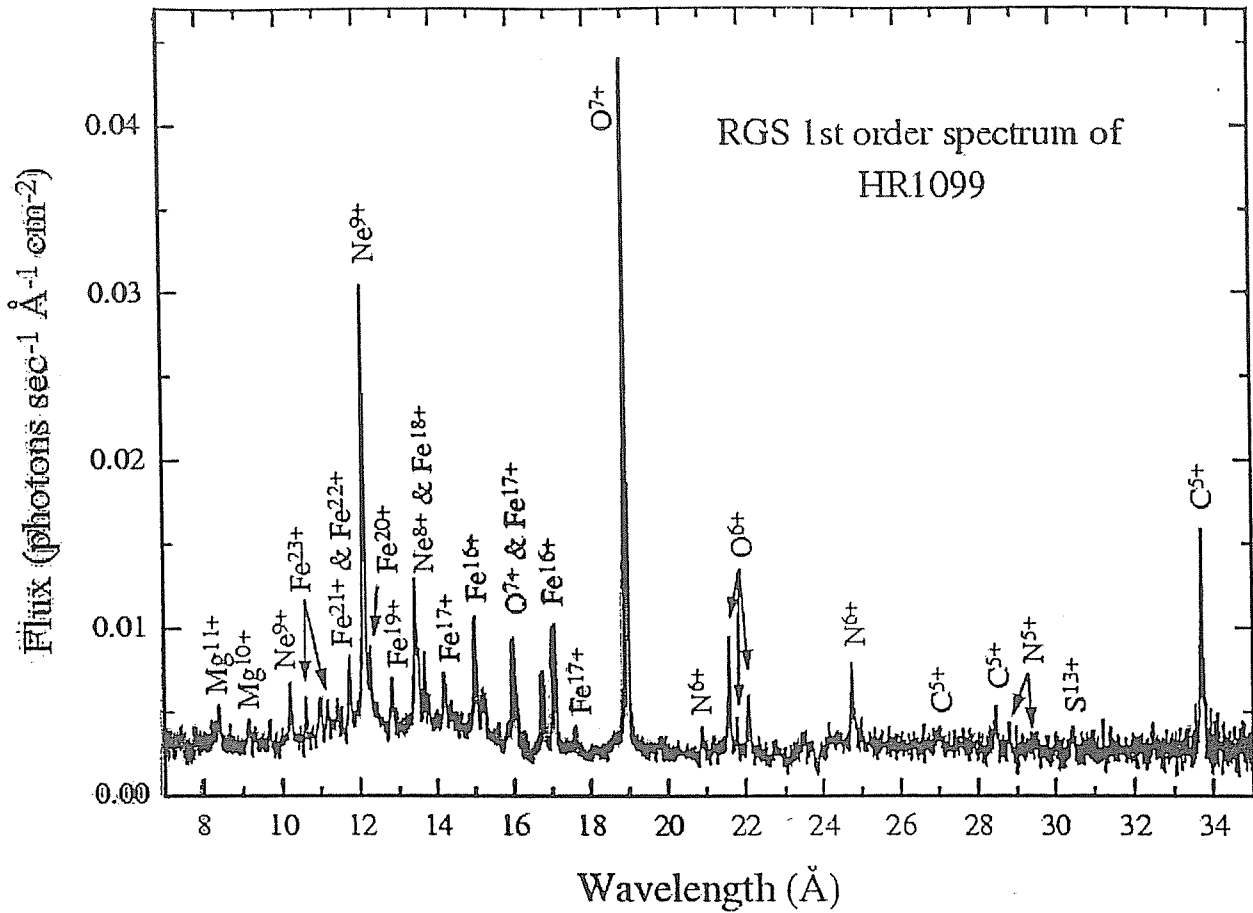
Camizares et al.,
2000, ApJ, 539, L41.

↑
dominated by Fe L

- He-like O: $n \sim n_{crit}$!
- T-distribution from ionization balance.

Similarly: HR1099 with XMM-Newton RGS

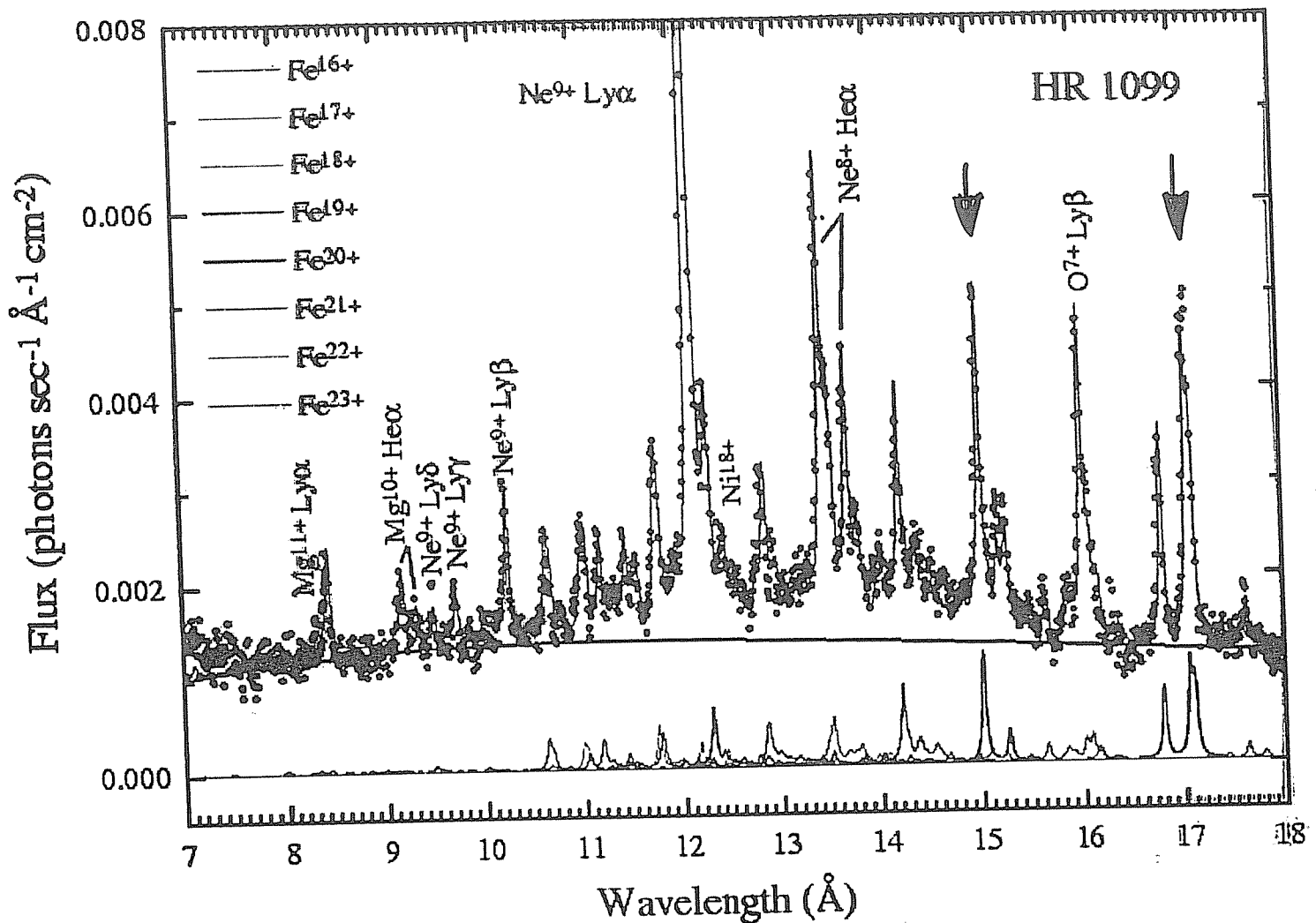
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Brinkman & al., 2001, A&A, 365.

- most FeL lines are $n=2-3$
($2p-3d$)
- line strengths: direct excitation;
tiny bit recombination into upper level;
excitation to higher levels + cascading

How well can we quantitatively calculate emission from a collisional plasma?



(Brinkman & et, 2001; courtesy Ehud Behar)

● pretty close fit! some questions remain regarding emission line ratios in Fe XVII .

● various calculations/compilations:

"Raymond-Smith" \rightarrow APEC

"Mekal" = Mewe / kaastra / hédahl

(NB public version not fully up to date)

Ehud Behar @ Columbia

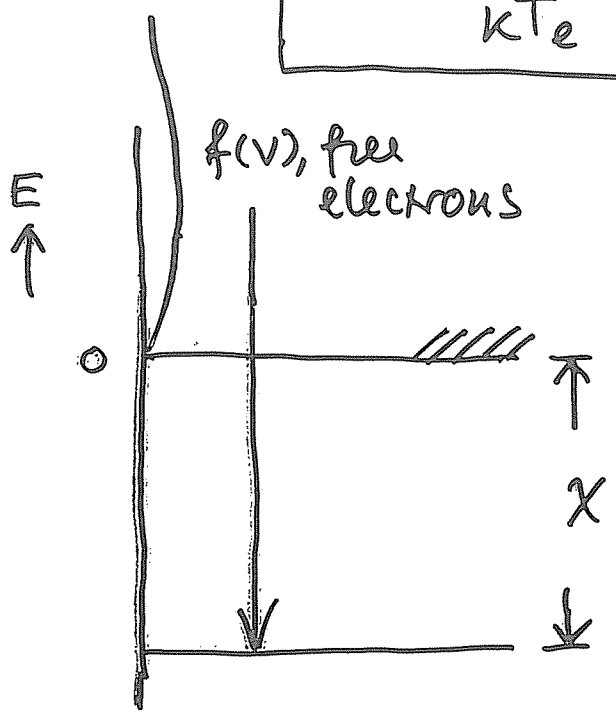
ALL: IONIZATION BALANCE \otimes COLLISIONAL RATES

6. PHOTOIONIZED PLASMA'S : DIAGNOSTICS.

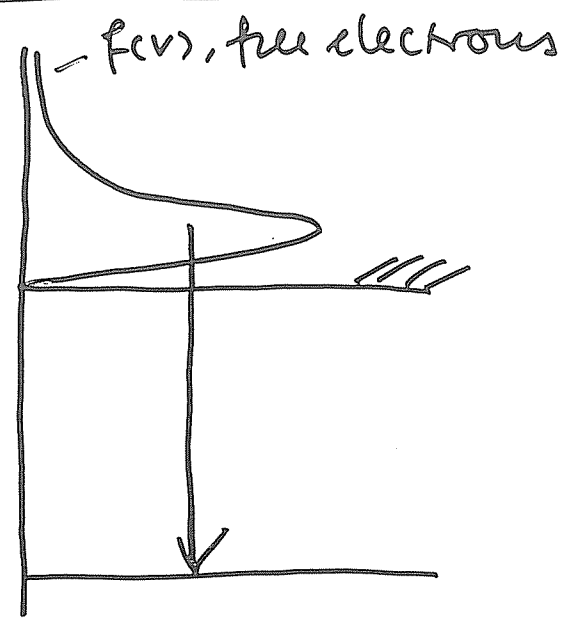
- inherently more complicated than collision-dominated case:
 - ① thermal + ionization balance ^{coupled}
 - ② ionization balance needs large amount of DR rate data (NB: plasma cool: DR very important)
 - ③ emission line power: have to solve rate equations for all cascades following recombination into excited states.
 - ④ by its very nature: radiative transfer much more likely to be important!
 - Unusual individual diagnostics (no terrestrial experiments! cf. Tokamaks, Atomic bombs)
- ⇒ but collisional & recombination spectra easy to distinguish!

diagnostic 1: kT_e directly

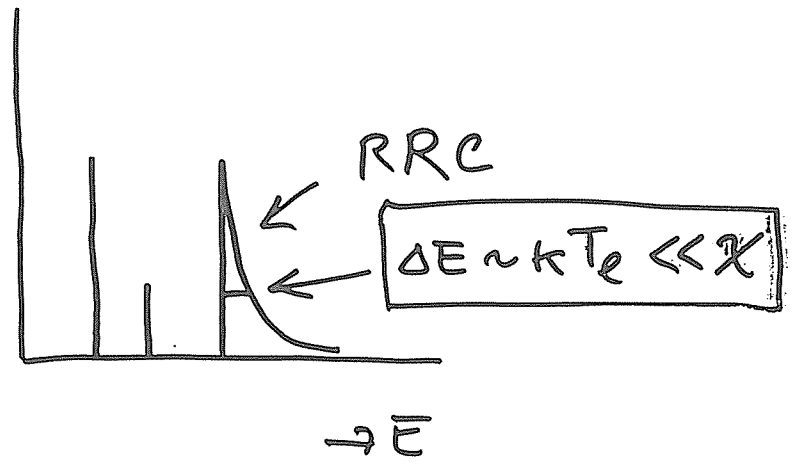
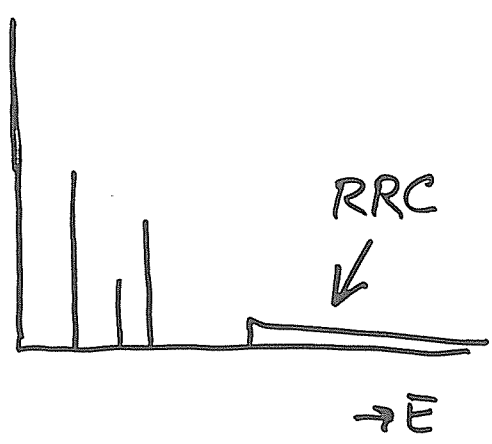
photoionized gas is COOL:
 $kT_e \ll \chi$



COLLISIONAL



PHOTOIONIZED

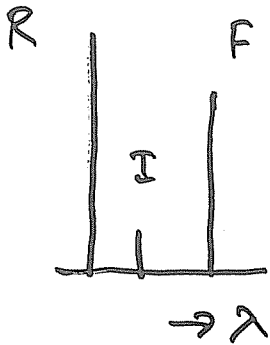


- seen in SN 1987A (Balmer jump; gas has cooled substantially)
- reinvented by Duane Liedahl (priority goes to Dick McCray)
- and subsequently seen in X-rays in Cyg X-3

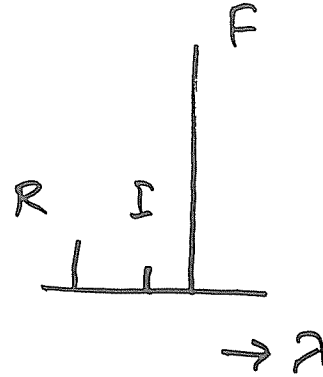
diagnostic 2:

- He-like ions: recombination: $F \gg I, R$

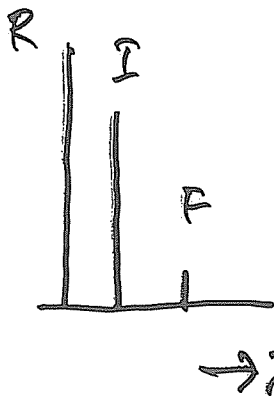
collisional



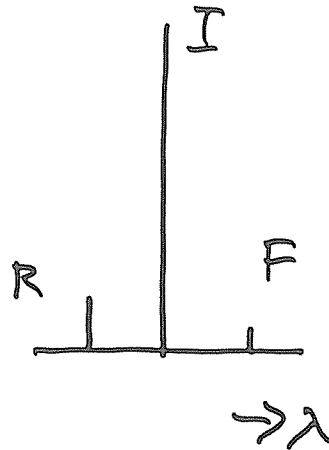
recombination



- density diagnostic still operates!



$n_e \gg n_{crit}$:
 $F \rightarrow I$



seen in LMXB spectra:
 Jean Cottam et al., 2001,
 A&A, 365
 (EXO 0748, 401822)

diagnostic 3:

- Fe L recombination power \ll collisional -
 \Rightarrow low Z K shells BRIGHTER than Fe L power

7. OTHER DIAGNOSTICS & FUN STUFF

37.

- collisional gas : coronae, SNR, ISM, clusters, IGM (?)
- recombination dominated spectra:
 - accretion dominated sources (XRB, AGN)

? Radiative transfer effect (resonance scattering) in strong emission lines from hot gas in clusters

⇒ $H\alpha$, D_A without SZ!

? GRB afterglow spectroscopy : weak evidence for Fe K ; excitation mech. unknown ⇒ X-ray redshifts ; chemical composition → progenitor?

? Dense plasmas : neutron star atmospheres, M-R relation

? Absorption spectroscopy IGM ?

? Find the warm IGM in emission w/ narrow-band imaging?

⋮